

### Abstract

The realization of Majorana corner modes generally requires unconventional superconducting pairing or s-wave pairing. However, the bulk nodes in unconventional superconductors and the low  $T_c$  of s-wave superconductors are not conducive to the experimental observation of Majorana corner modes. Here, we show the emergence of a Majorana corner mode at each corner of a two-dimensional topological insulator in proximity to a  $d+id'$  pairing superconductor, such as heavily doped graphene or especially a twisted bilayer of a cuprate superconductor, e.g.,  $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ , which has recently been proposed as a fully gapped chiral  $d_{x^2-y^2}+id_{xy}$  superconductor with  $T_c$  close to its native 90 K, and an in-plane magnetic field. By numerical calculation and intuitive edge theory, we find that the interplay of the proximity-induced pairing and Zeeman field can introduce opposite Dirac masses on adjacent edges of the topological insulator, which creates one zero-energy Majorana mode at each corner. Our scheme offers a feasible route to achieve and explore Majorana corner modes in a high-temperature platform without bulk superconductor nodes.

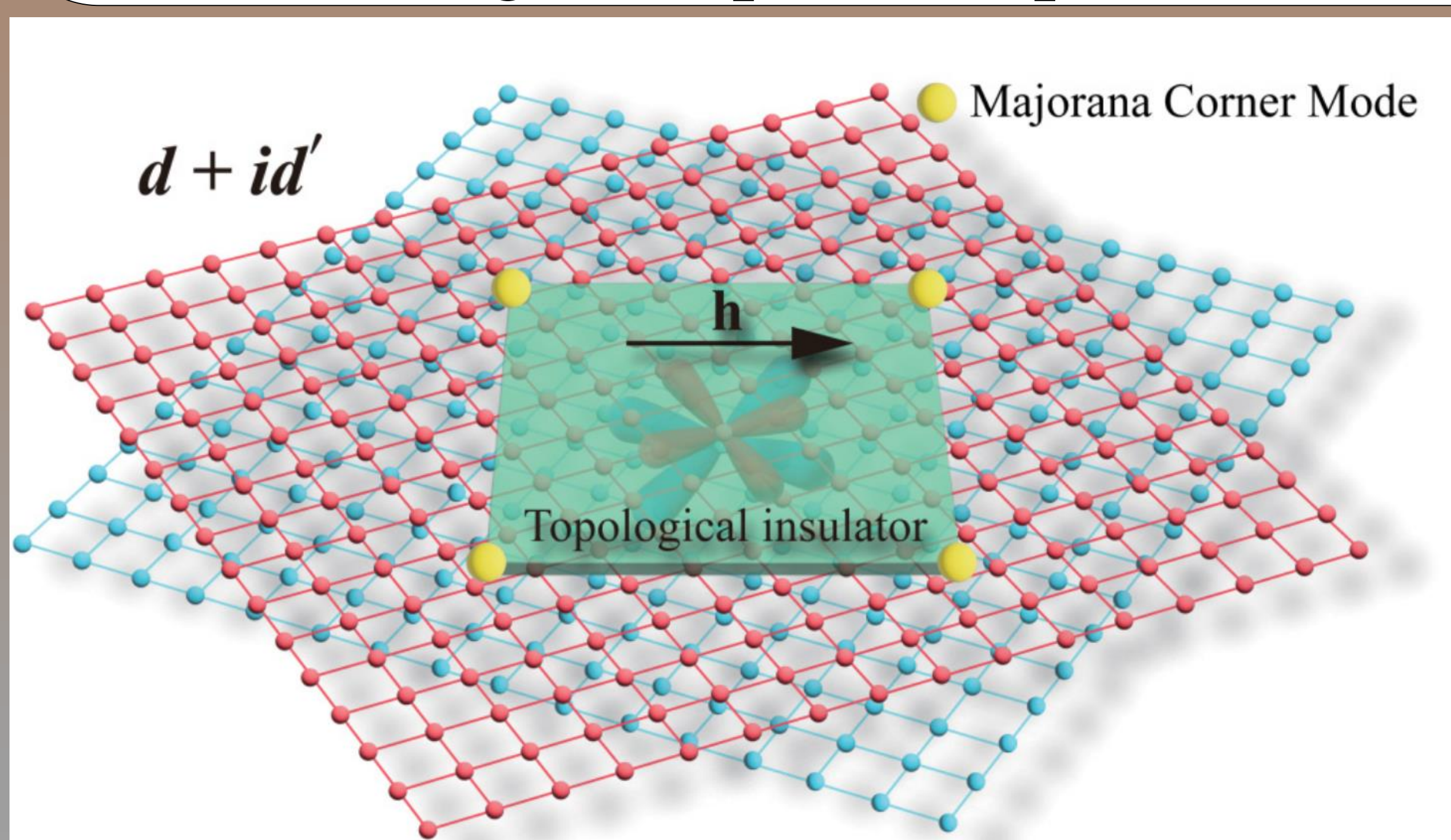


FIG. 1. Schematic diagram of the proposed setup. A heterostructure composed of a 2D topological insulator deposited on a high- $T_c$  fully gapped  $d + id'$  pairing superconductor such as a twisted bilayer of cuprate superconductor monolayers and subject to an in-plane Zeeman field. The sphere at each corner represents one zero-energy Majorana corner mode.

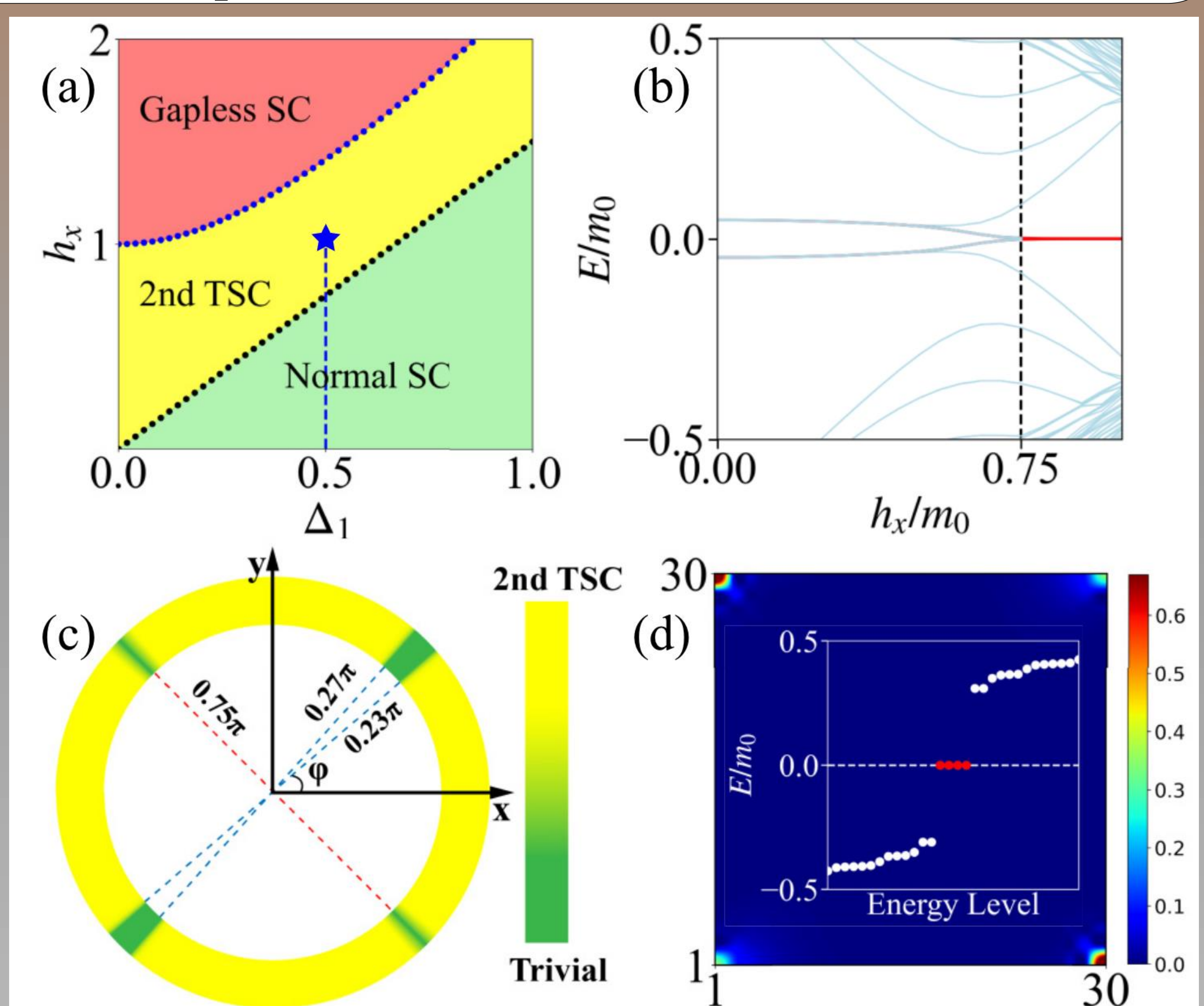


FIG. 3. (a) Phase diagram vs  $h_x$  and  $\Delta_1$ . (b) Line-scan real-space spectra along the blue dashed line in (a).  $\mu = 0.1$ . (c) Phase diagram as a function of the azimuth of the in-plane Zeeman field. Parameters are  $h_{\parallel} = m_0$ ,  $h_x = h_{\parallel} \cos \varphi$ ,  $h_y = h_{\parallel} \sin \varphi$ ,  $\mu = 0$ . (d) Energy spectrum of the real-space TB Hamiltonian at  $\varphi = 0.4\pi$ ,  $\mu = 0.1$  for a  $30 \times 30$  square size sample. The density plot exhibits the corner localized probability distribution of the four zero-energy MCMs.

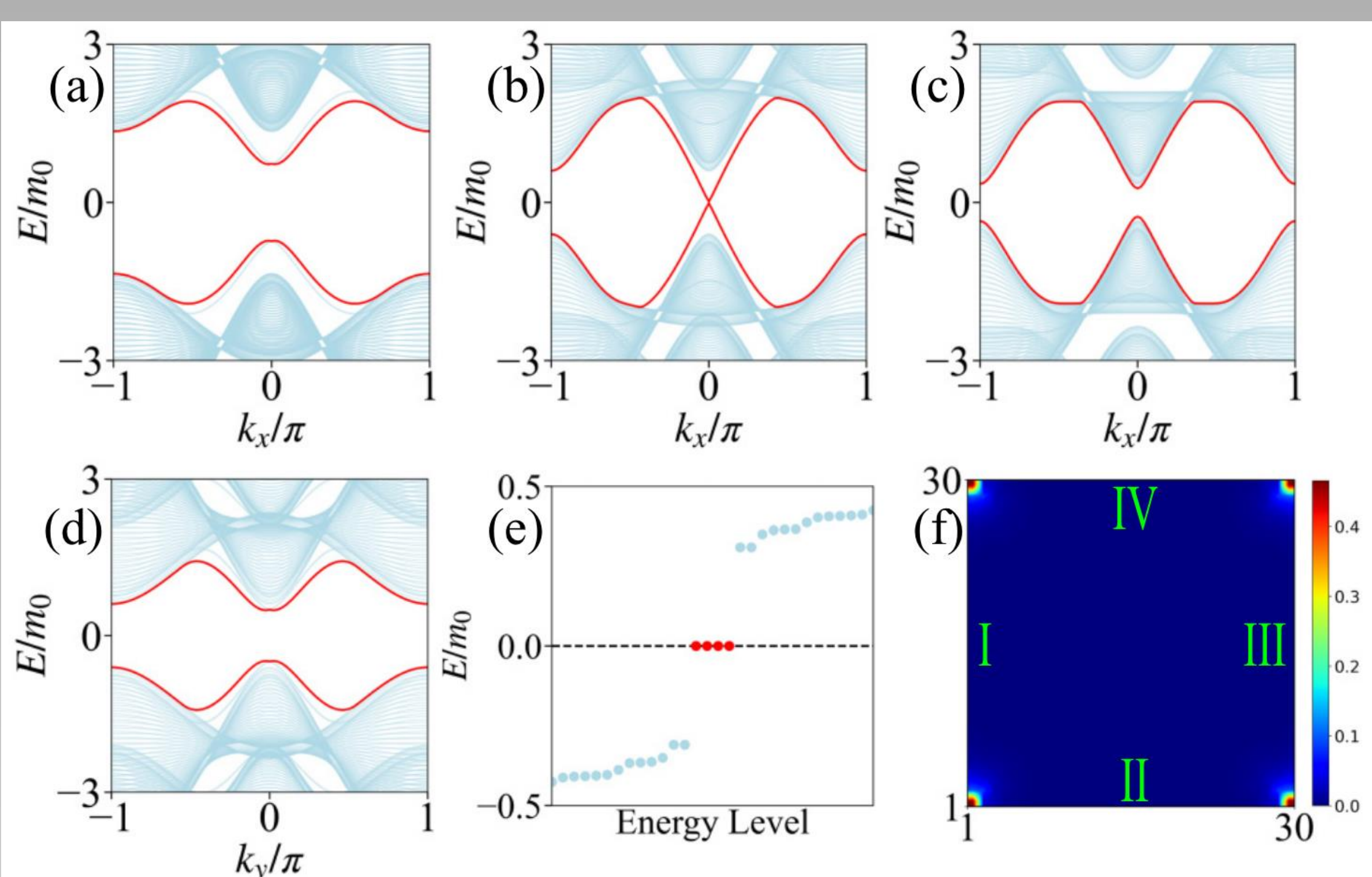


FIG. 2. Quasiparticle bands with edge spectra (red lines) and bulk spectra (light blue lines) for an open boundary condition along the  $y$  direction for (a)  $h_x = 0$ , (b)  $h_x = 0.75$ , and (c)  $h_x = 1$ . The gap for the edge spectrum closes at the critical Zeeman field  $h_x = 0.75$ . (d) Quasiparticle bands with the edge spectrum (red lines) and bulk spectra (light blue lines) for open boundary conditions along the  $x$  direction with the critical Zeeman field  $h_x = 0.75$ . (e) Eigenvalues of the real-space TB Hamiltonian with  $h_x = 1$  for a  $30 \times 30$  square size sample. (f) The density plot displays the corner localized probability distribution of the four zero-energy MCMs in (e). I, II, III, and IV label the four edges. Common parameters are  $m_0 = 1$ ,  $t_x = t_y = \lambda_x = \lambda_y = 2$ ,  $\Delta_1 = \Delta_2 = 0.5$ ,  $\mu = 0.1$ .

In conclusion, we have demonstrated that a heterostructure composed of topological insulators and twisted bilayer cuprate superconductors can host MCMs when an in-plane Zeeman field is applied. Our proposed setup with fully gap pairing and high transition temperature has great advantages for the experimental observation of the zero-energy MCM signals. Our work may also stimulate further studies of MCMs in twisted systems.