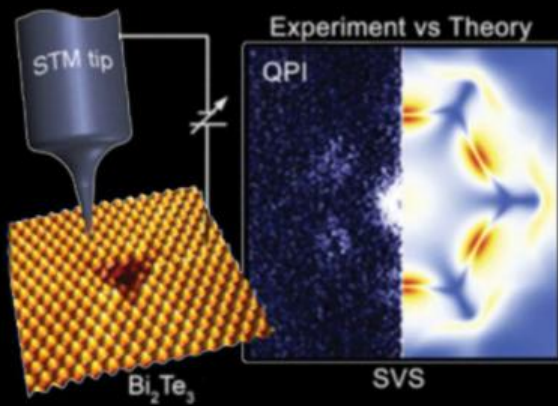
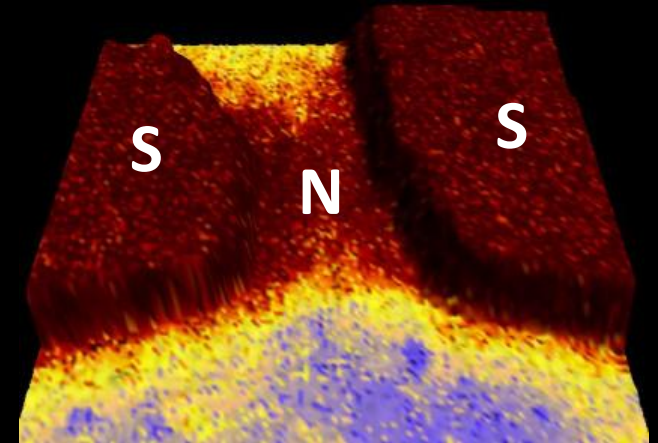


BIT MIPT Summer school 17-24 July 2023



Prof Vasily Stolyarov





Golubov Lab



Stolyarov Lab



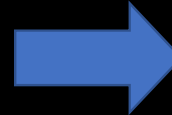
Pogosov Lab



Bobkov's Lab



Like in Manchester but Advanced ...



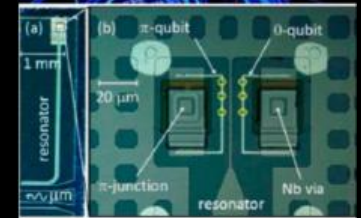
Stolyarov center

Superconducting Quantum technology

Superconducting Digital electronics

Superconducting Neuromorphic systems

Topologically protected systems

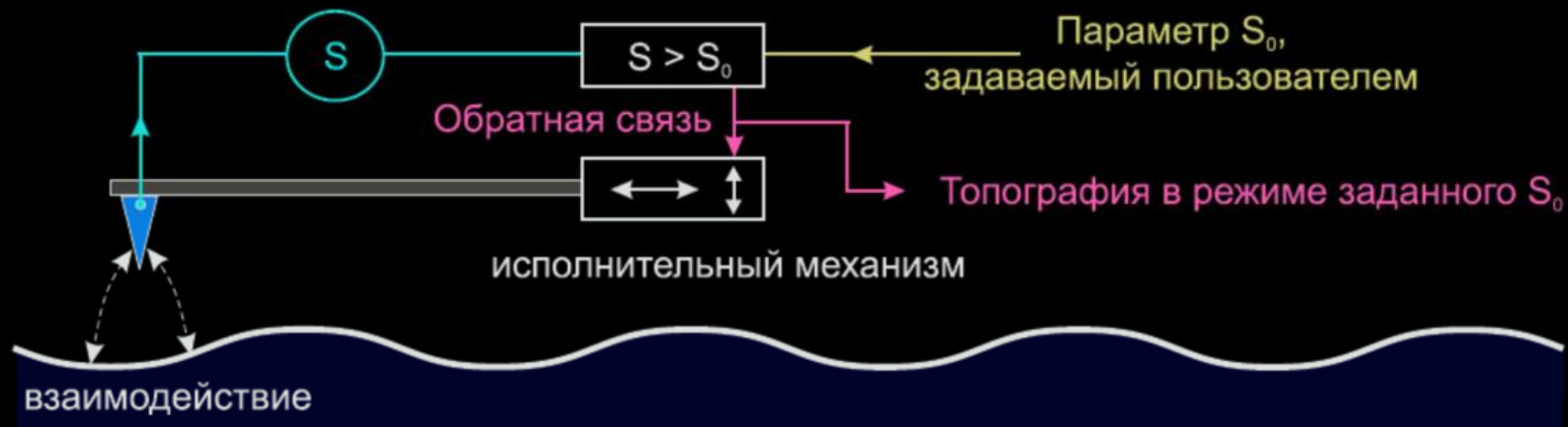


Cryogenic Scanning probe microscopy for superconducting heterostructures

Cryogenic Scanning probe microscopy for superconducting heterostructures

- Scanning Tunneling Microscopy: STM, STS, spin-polarized STM
- Scanning Atomic Force Microscopy: AFM, MFM, Kelvin probe, Force probe...
- Nearfield Scanning Optic Microscopy: NSOM
- Nearfield Scanning RF Microscopy
- Hall probe Microscopy or SQUID Microscopy
- Scanning Laser Microscopy
- Scanning Electron Microscopy

Cryogenic Scanning probe microscopy for superconducting heterostructures



Cryogenic Scanning Tunneling Microscopy

Introduction

Invention of Scanning Tunneling Microscope



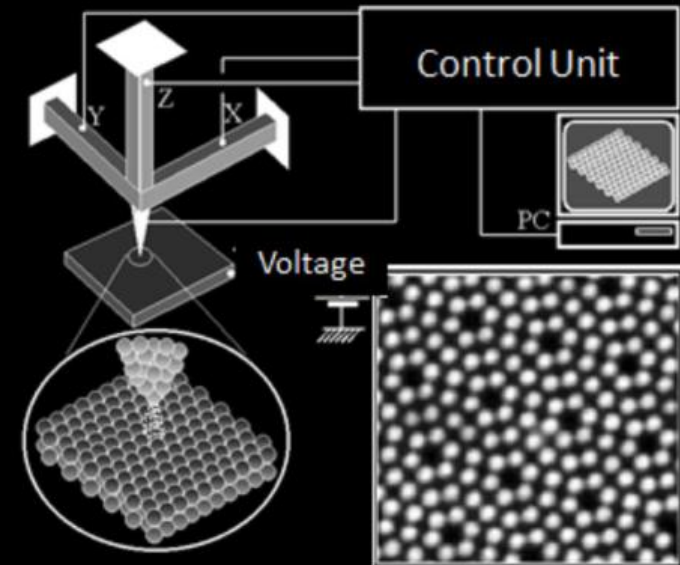
Ernst Ruska



Gerd Binnig

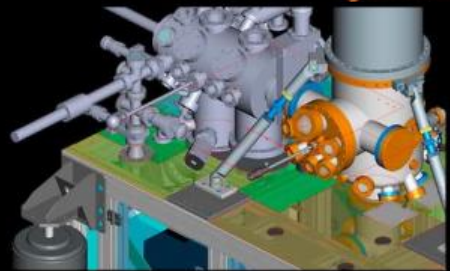
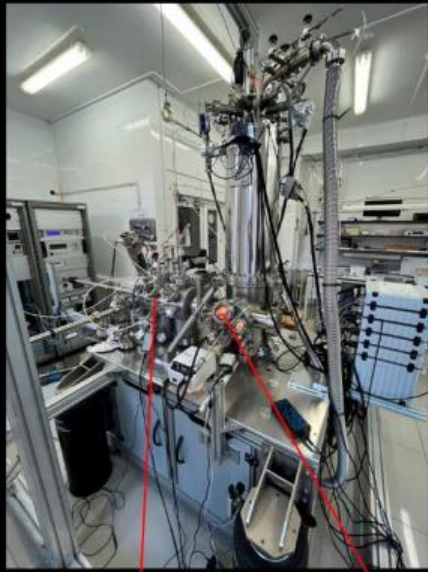


Heinrich Rohrer

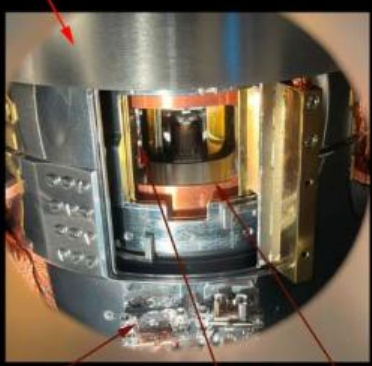


The Nobel Prize in Physics 1986: to Ernst Ruska *"for his fundamental work in electron optics, and for the design of the first electron microscope »* and to Gerd Binnig and Heinrich Rohrer *"for their design of the scanning tunneling microscope"*.

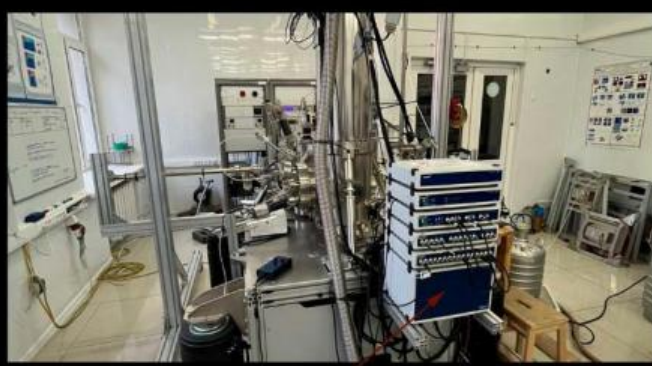
- JT-STM SPECS (Joule-Thomson Scanning Tunneling Microscope)
- $P \leq 10^{-10}$ mbar, $T = 1.2$ K,
- Magnetic Field up to 3 T
- Scanning area 2 mkm^2



две позиции



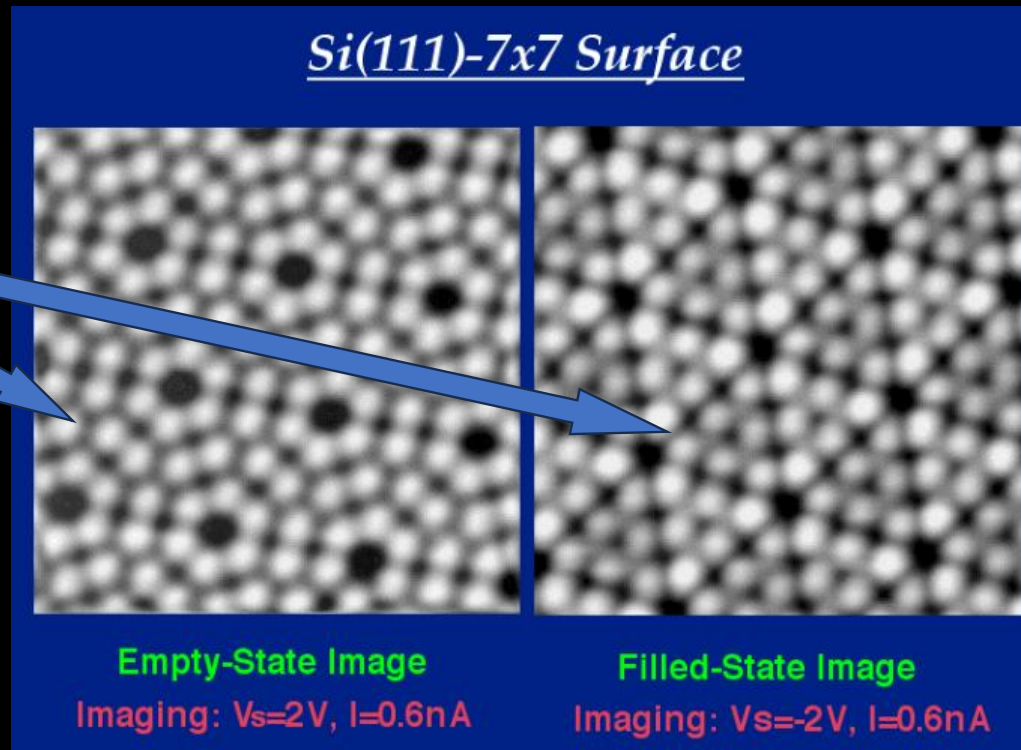
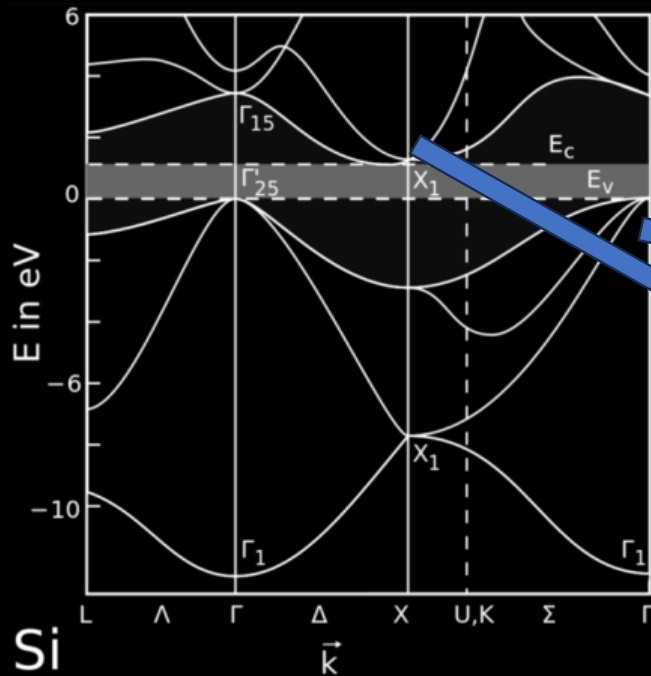
Держатели образцов 77K Держатель для скола при 4.2K



Магнит на 3T

Блок электроники Nanonis

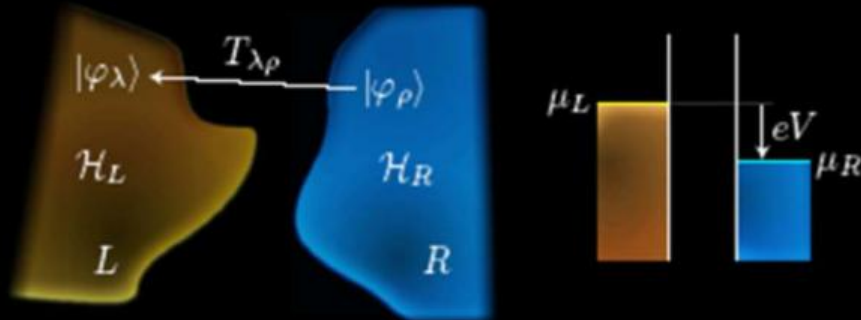
Imaging of valence and conduction states in a semiconductor



The images depend on the applied voltage.

This is a spectroscopic effect, **what do we measure exactly with STM?**

Tunneling spectroscopy



The Fermi golden rule is used in deriving the tunneling current.

Fermi's golden rule is a formula that describes the transition rate (the probability of a transition per unit time) from one energy eigenstate of a quantum system to a group of energy eigenstates in a continuum, as a result of a weak perturbation.

Consider the tunneling rate $t_{\lambda\rho}$ between the two state at left and right systems described by $|\varphi_\lambda\rangle$ and $|\varphi_\rho\rangle$.

The probability of transition from state λ to state ρ per unit time is:

$$t_{\lambda\rho} \propto |M_{\lambda\rho}| \delta(E_\lambda - E_\rho)$$

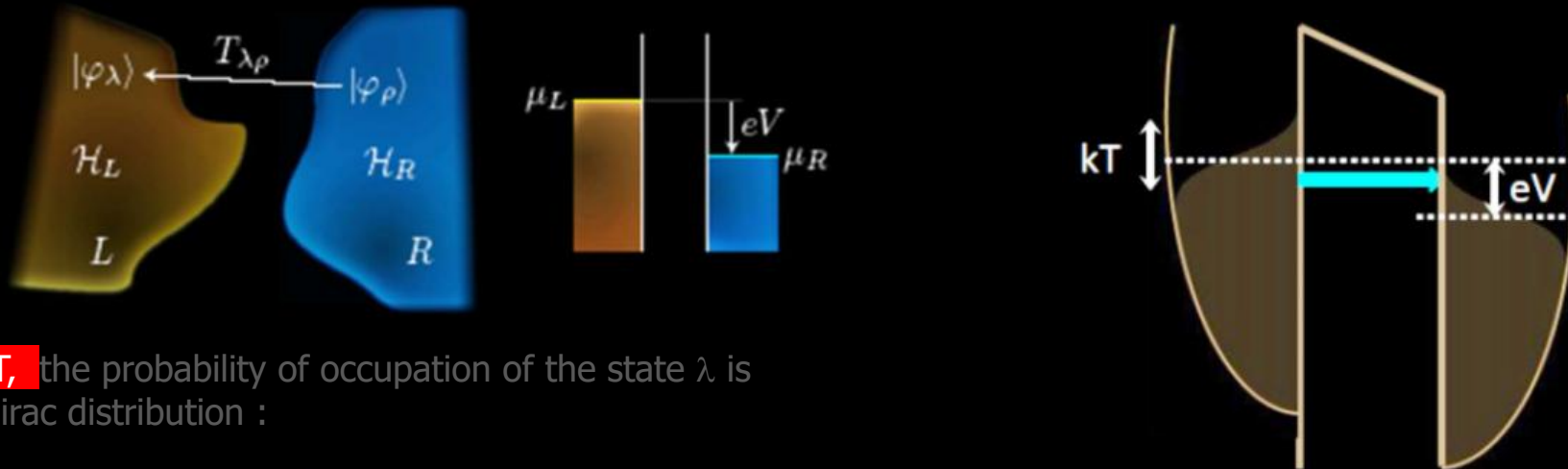
Where :

$$M_{\lambda\rho} = \langle \varphi_\lambda | V | \varphi_\rho \rangle$$

$$M_{\lambda\rho} = \int \varphi_\lambda^*(\vec{r}) V(\vec{r}) \varphi_\rho(\vec{r}) d^3\vec{r}$$

Here $V(r)$ is the mutual perturbation of the two systems

Tunneling spectroscopy



At finite temperature T , the probability of occupation of the state λ is given by the Fermi-Dirac distribution :

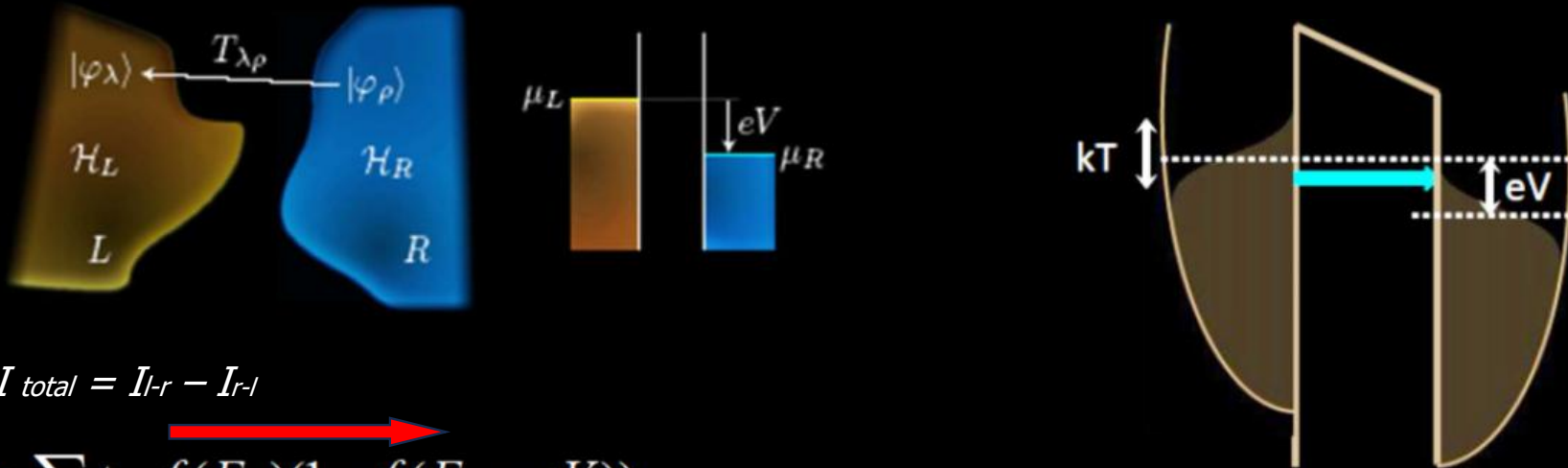
$$f(E_\lambda) = \frac{1}{1 + \exp((E_\lambda - \mu_\lambda) / kT)}$$

– μ_λ is the chemical potential (Fermi level)

The current of electrons from left to right is proportional to the probability that the state λ is occupied $f(E_\lambda)$ and the probability that the state ρ is empty $(1-f(E_\rho))$

$$I_{l-r} \propto \sum_{\lambda\rho} t_{\lambda\rho} f(E_\lambda)(1 - f(E_\rho - eV))$$

Tunneling spectroscopy



The total current $I_{total} = I_{l-r} - I_{r-l}$

$$I_{l-r} \propto \sum_{\lambda\rho} t_{\lambda\rho} f(E_\lambda)(1 - f(E_\rho - eV))$$

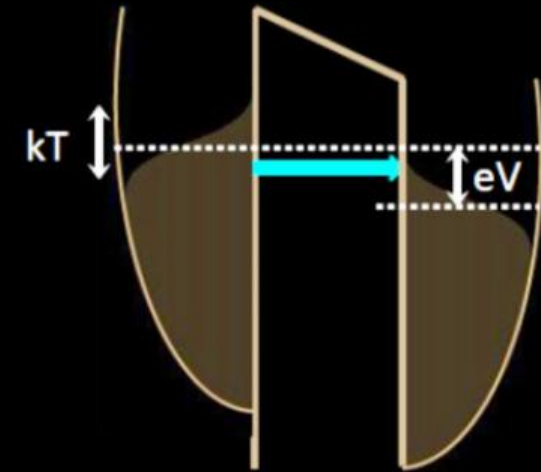
$$I_{r-l} \propto \sum_{\lambda\rho} t_{\lambda\rho} (1 - f(E_\lambda))f(E_\rho - eV)$$

$$t_{\lambda\rho} \propto |M_{\lambda\rho}| \delta(E_\lambda - E_\rho)$$

$$I_{total} \propto \sum_{\lambda\rho} |M_{\lambda\rho}| (f(E_\lambda) - f(E_\rho - eV)) \delta(E_\lambda - E_\rho)$$

Calculation of the matrix element for an idealized STM tip

The problem is how to calculate $M_{\lambda\rho} = \int \phi_{\lambda}^*(\vec{r})V(\vec{r})\phi_{\rho}(\vec{r})d^3\vec{r}$?



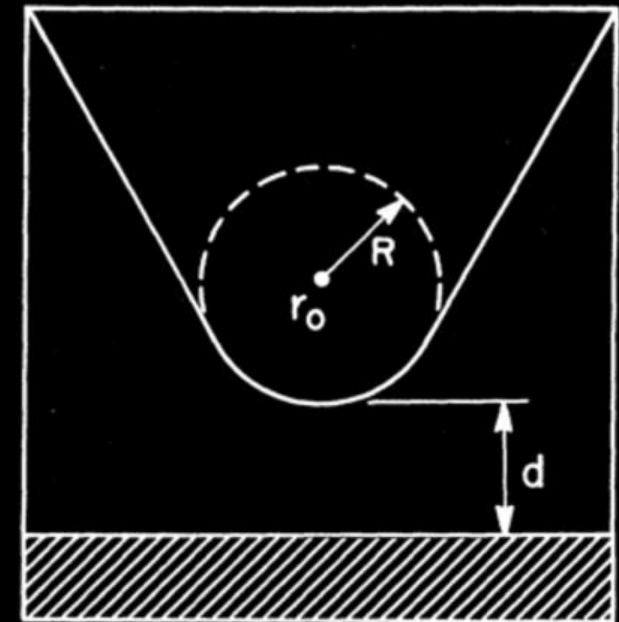
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Tersoff and Hamann demonstrate that for a tip with a local spherical potential at the apex:

$$M_{\lambda\rho} \propto M_0 \varphi_{\lambda}(\vec{r}_0)$$

$\vec{r}_0 = (x, y, z_0)$ - position of the last atom of the tip



(Phys. Rev. Letters 50, 1998 (1983); PRB 31, 805 (1985))

Calculation of the matrix element for an idealized STM tip

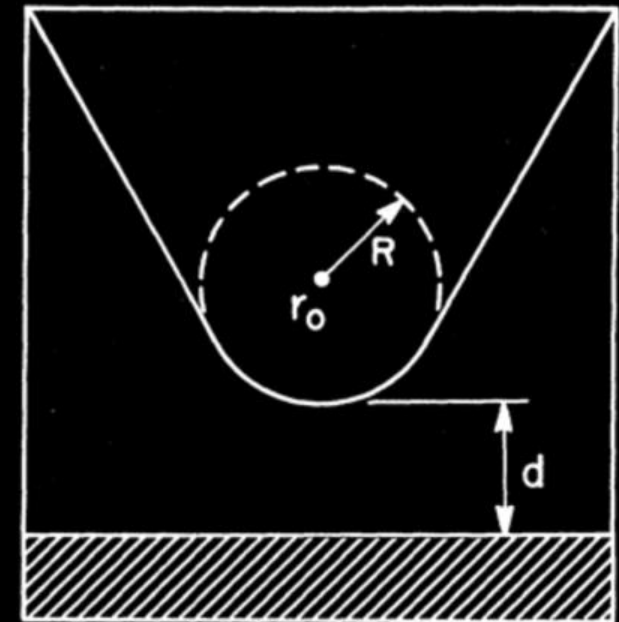
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By replacing the $\Sigma_{\lambda\rho}$ - by the integral over all energies $d\omega$, we can write, within Tersoff and Hamann's approximation



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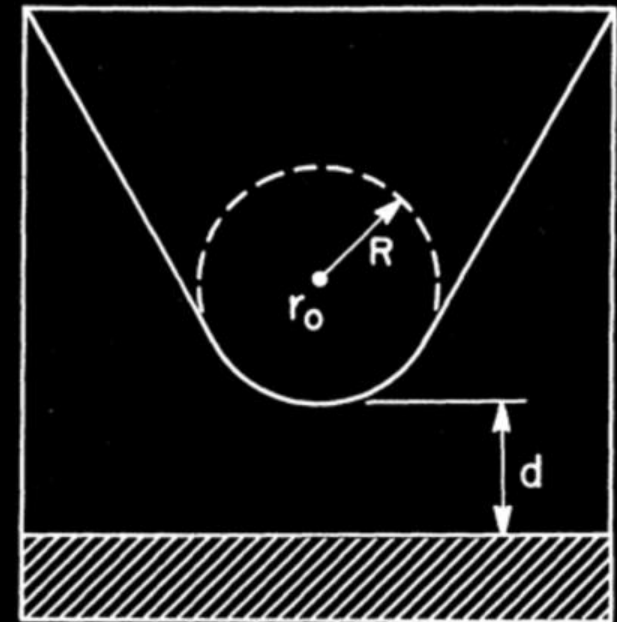
By replacing the $\Sigma_{\lambda\rho}$ by the integral over all energies $d\omega$, we can write, within Tersoff and Hamann's approximation

$$I_{total}(\vec{r}_0, V) \propto M_0^2 \int \sum_\lambda |\varphi_\lambda(\vec{r}_0)|^2 \delta(E_\lambda - \omega) (f(\omega) - f(\omega - eV)) d\omega$$

The value

$$\rho(\vec{r}_0, \omega) \propto \sum_\lambda |\varphi_\lambda(\vec{r}_0)|^2 \delta(E_\lambda - \omega)$$

is known as **Local Density of States (LDOS)**



(Phys. Rev. Letters 50, 1998 (1983); PRB 31, 805 (1985))

!! The tunneling current vs bias contain the information about LDOS of the sample measured at the position of tip apex !!

Calculation of the tunneling current

In a more general case of a non-constant LDOS of the tip $\rho(r_0, E)$, the total current can write:

$$I_T(r, V) = \frac{4\pi e}{\hbar} \int_{-\infty}^{+\infty} |M|^2 [f(\omega - eV) - f(\omega)] \rho_t(r_0, \omega - eV) \rho_s(r, \omega) d\omega$$

↙ DOS of tip ↘ DOS of sample

Often, the tunneling conductance, $\frac{\partial I_T(r, V)}{\partial V}$ is measured/studied :

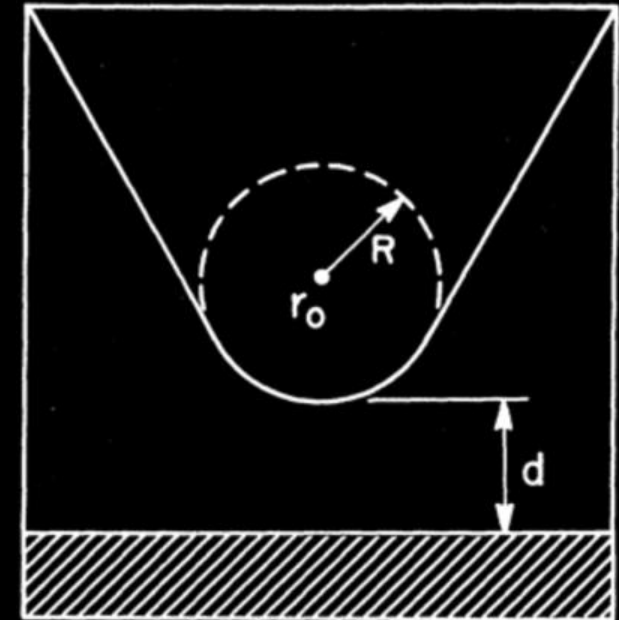
$$\frac{\partial I}{\partial V} \propto \int \rho_S(\omega) \frac{\partial \rho_T(\omega - eV)}{\partial V} [f(\omega - eV, T) - f(\omega, T)] d\omega +$$

$$+ \int \rho_S(\omega) \rho_T(\omega - eV) \frac{\partial f(\omega - eV, T)}{\partial V} d\omega$$

It looks complicate, but it is a folding integral within the unknown LDOS of the sample.

If in the bias window of interest $\rho_t(r_0, \omega) = cte$, then:

$$\frac{\partial I_T(r, V)}{\partial V} = \frac{4\pi e}{\hbar} \rho_t(r_0, \omega) |M|^2 \int_{-\infty}^{+\infty} \rho_s(r, \omega) \frac{\partial f(\omega - eV)}{\partial V} d\omega$$



(Phys. Rev. Letters 50, 1998 (1983); PRB 31, 805 (1985))

1957: Microscopic Theory of Superconductivity (BCS)

(Nobel prize: 1972)



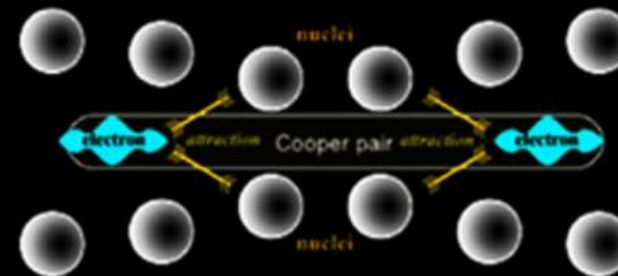
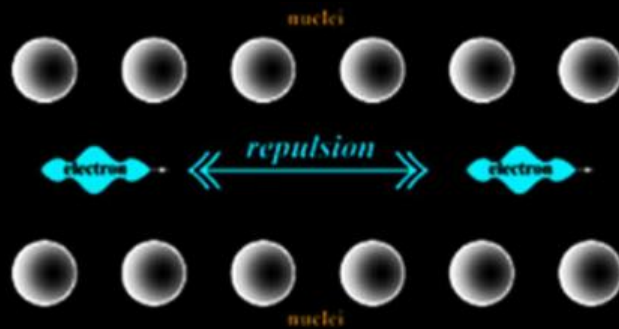
John Bardeen



Leon Neil Cooper



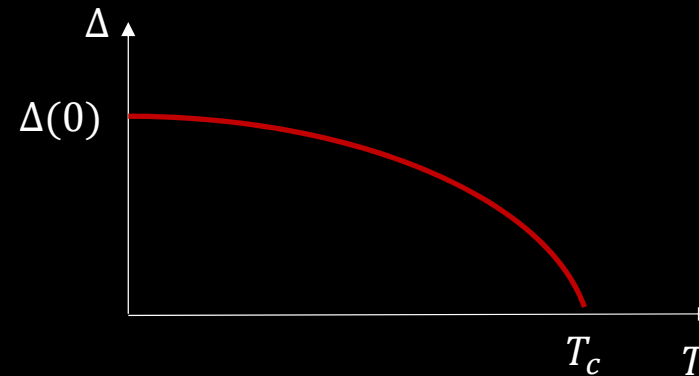
John Robert Schrieffer



Conventional (BCS) superconductor:
Gap 2Δ in the excitation spectrum:

$$\rho_s(\omega)_{BCS} = \frac{E}{\sqrt{E^2 - \Delta(T)^2}}$$

$$\frac{2\Delta(0)}{k_B T_c} = 3.52$$



$$\frac{\partial I_T(r, V)}{\partial V} = \frac{4\pi e}{\hbar} \rho_t(r_0, \omega) |M|^2 \int_{-\infty}^{+\infty} \rho_s(r, \omega) \frac{\partial f(\omega - eV)}{\partial V} d\omega$$

1960: Quantum Tunneling, Gap, Signatures of Electron-Phonon Interaction



Leo Esaki

Ivar Giaever

Brian Josephson

The Nobel Prize in Physics 1973 *"for their experimental discoveries regarding tunneling phenomena in semiconductors and superconductors, respectively"* and *"for his theoretical predictions of the properties of a supercurrent through a tunnel barrier, in particular those phenomena which are generally known as the Josephson effects"*.

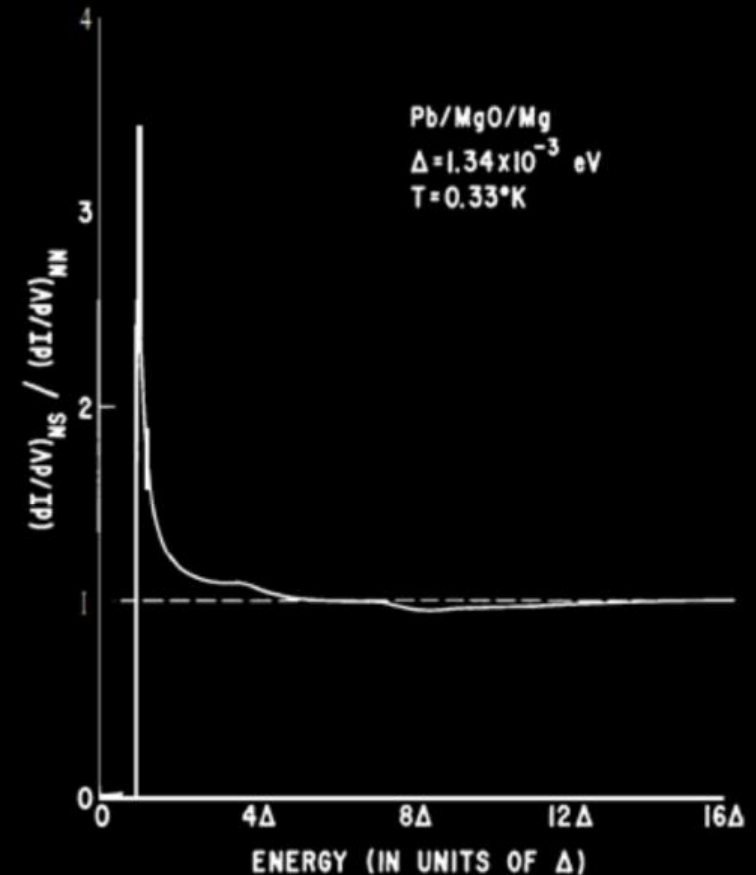
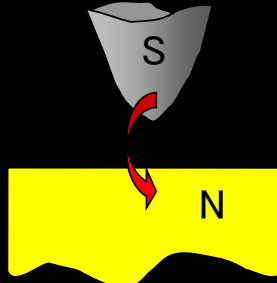


Fig. 12.
A normalized derivative of the current with respect to voltage of a lead junction at low temperature. The simple BCS-theory predicts that the derivative should approach unity asymptotically as the energy increases. Instead several wiggles are observed in the range between 4Δ and 8Δ . These wiggles are related to the phonon spectrum in lead.

Tunneling into a Superconductor

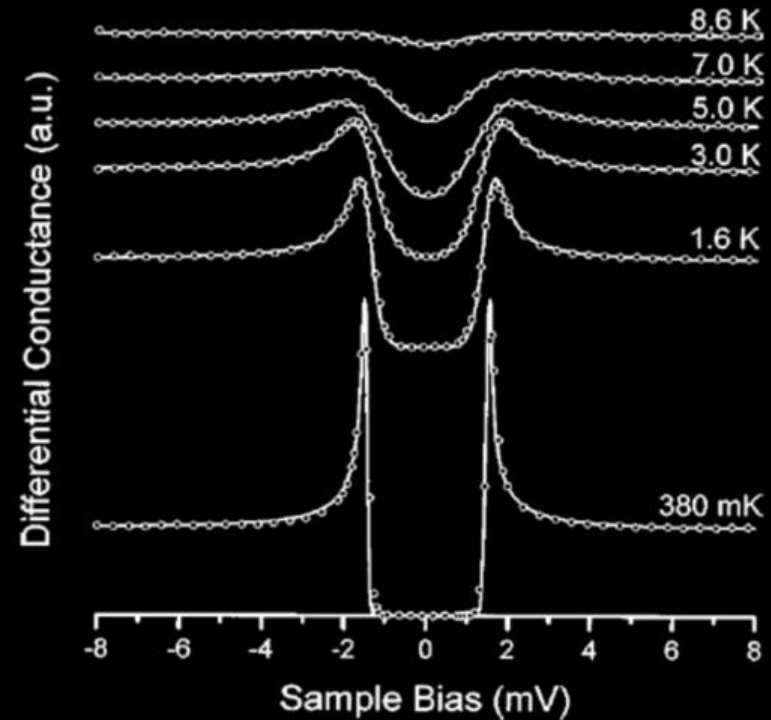


$$\frac{dI}{dV}(V) = -\frac{2\pi e^2 T}{h} N_p \int_{-\infty}^{\infty} N_S(E+eV) \frac{\partial f}{\partial E}(E) dE$$

BCS-kind Superconductor:
Gap 2Δ in the excitation spectrum:

$$N_S(E) = N(0) \frac{E}{\sqrt{(E^2 - \Delta^2)}}$$

BCS \rightarrow $\frac{2\Delta(0)}{k T_c} \approx 3.5$



Pan, Davis, Univ. de Berkeley. (APL, 1998)

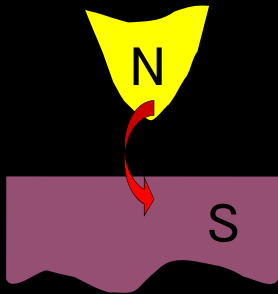
Scanning Tunneling Spectroscopy Study of the Proximity Effect in a Disordered Two-Dimensional Metal

L. Serrier-Garcia,¹ J. C. Cuevas,² T. Cren,^{1,*} C. Brun,¹ V. Cherkez,¹ F. Debontridder,¹
D. Fokin,^{1,3} F. S. Bergeret,⁴ and D. Roditchev¹

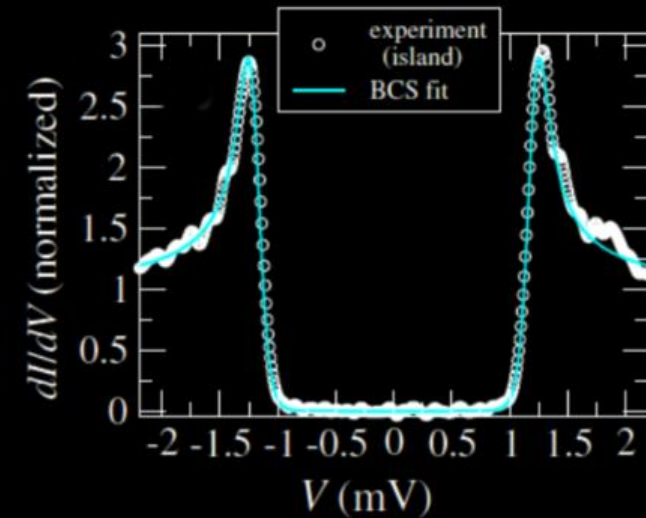
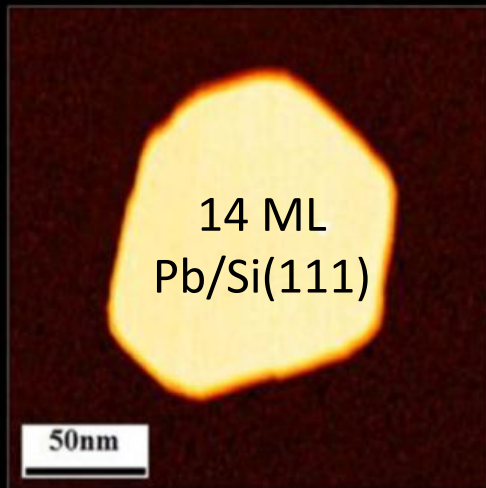
¹Institut des Nanosciences de Paris, Université Pierre et Marie Curie (UPMC) and CNRS-UMR 7588,
4 place Jussieu, 75252 Paris, France

$$dI/dV(\mathbf{r}) = \int_{-\infty}^{\infty} N_s(E, \mathbf{r}) \left[\frac{-\partial f(E + eV)}{\partial(eV)} \right] dE$$

Convolution



BSC DOS
$$N_S(E) = N_N(E) \frac{E}{\sqrt{E^2 - \Delta^2}}$$



$$\Delta = 1.20 \text{ meV } T_{\text{eff}} = 0.38 \text{ K}$$

Superconducting proximity effect

boundary



Superconductor

Non supercond.
metal

First experimental evidences

Holm and Meissner (1932)
Bedard and Meissner (1956)
Meissner (1958), (1960)

First theory

De Gennes (1964)
McMillan (1968)
Clarke (1969)
Deutscher and De Gennes (1969)

Superconducting proximity effect

boundary



Superconductor Non supercond. metal

In case of diffuse metal

$$L_T = \sqrt{\hbar D_N / (2\pi k_B T)}$$

Cooper pair density

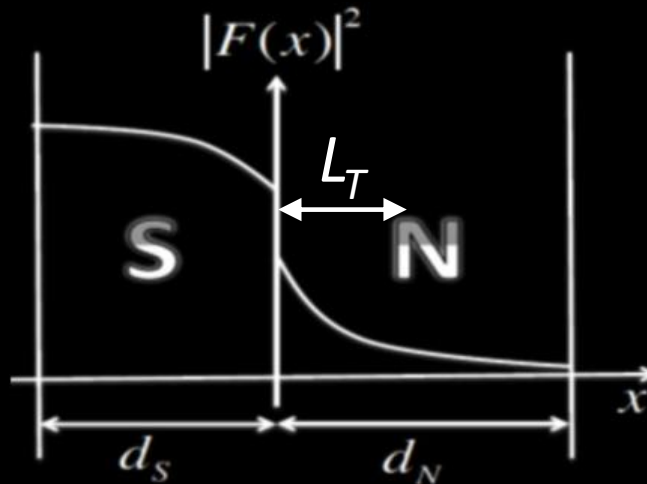
$$F(\vec{r}) = \langle \hat{\psi}_\uparrow(\vec{r}) \hat{\psi}_\downarrow(\vec{r}) \rangle$$

Order parametr:

$$\Delta(\vec{r}) = V(\vec{r})F(\vec{r})$$

First experimental evidences

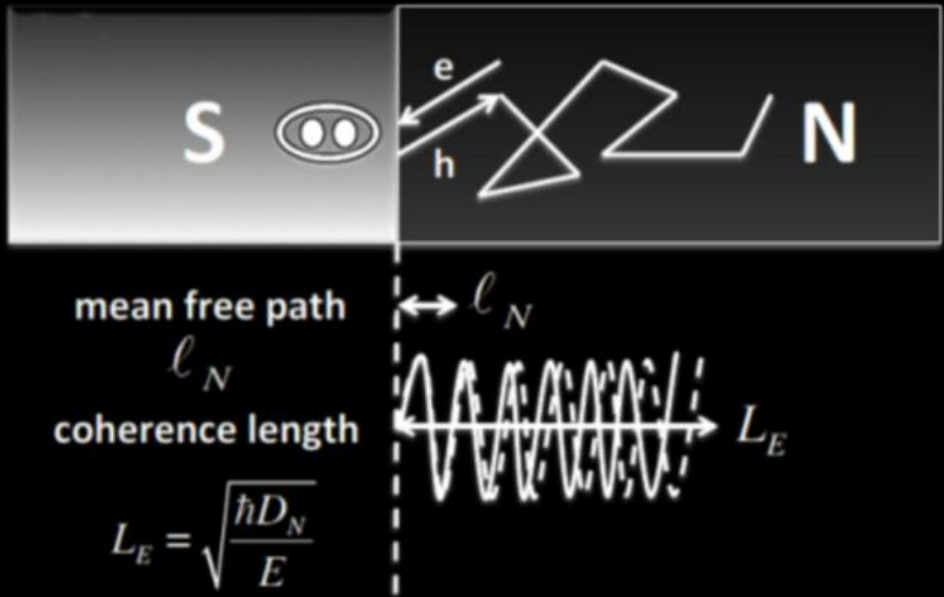
- Holm and Meissner (1932)
- Bedard and Meissner (1956)
- Meissner (1958), (1960)



First theory

- De Gennes (1964)
- McMillan (1968)
- Clarke (1969)
- Deutscher and De Gennes (1969)

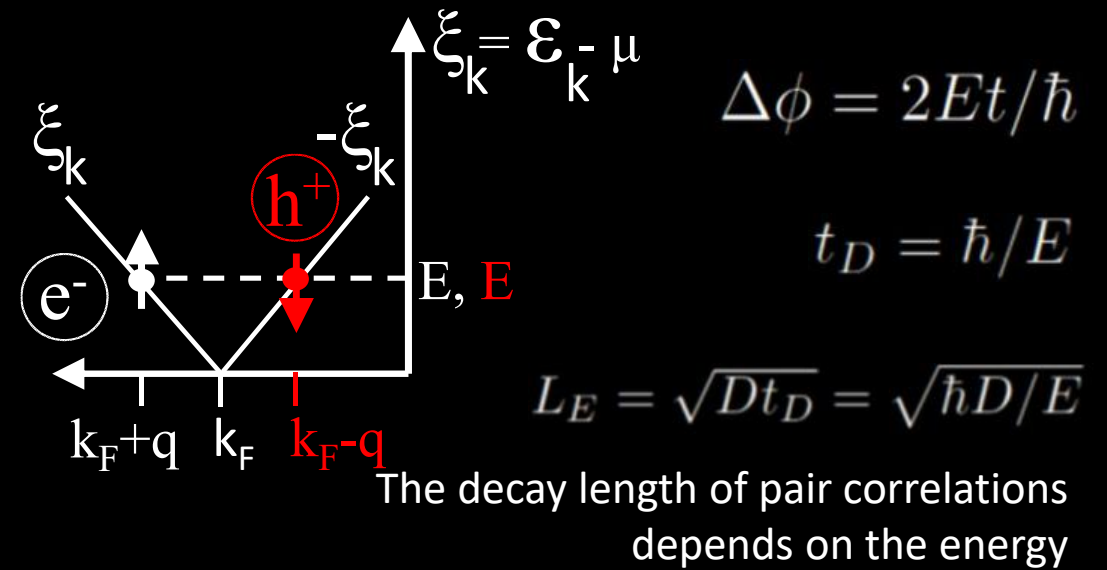
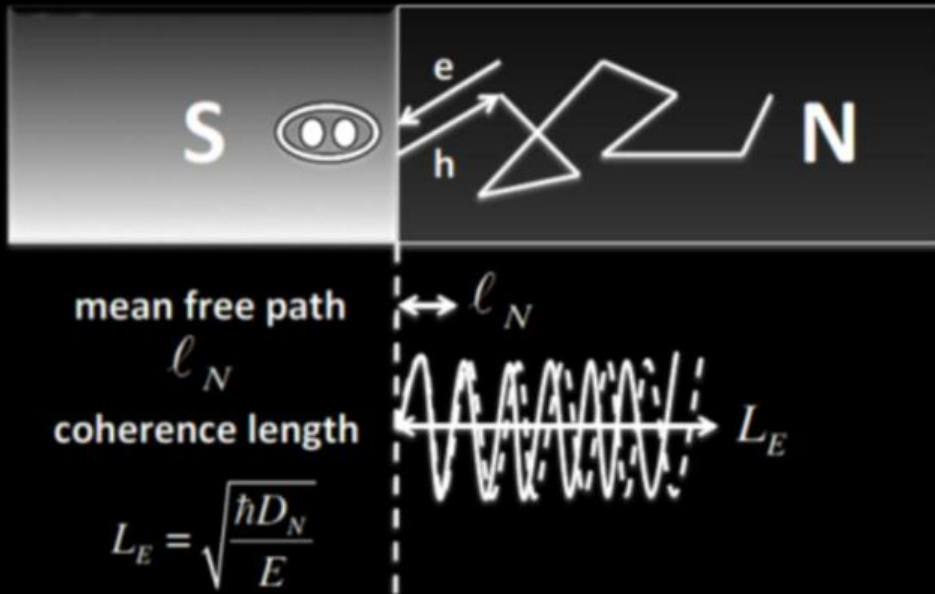
Andreev reflection at the S/N boundary + extended phase coherence in N



Andreev (1964),
 Eilenberger (1968),
 Usadel (1970),
 Eliashberg (1971)

Larkin *et al.* (1968,75,77),
 Schmid & Schön (1975),
 Blonder *et al.* (1982),
 Zaitsev (1984)

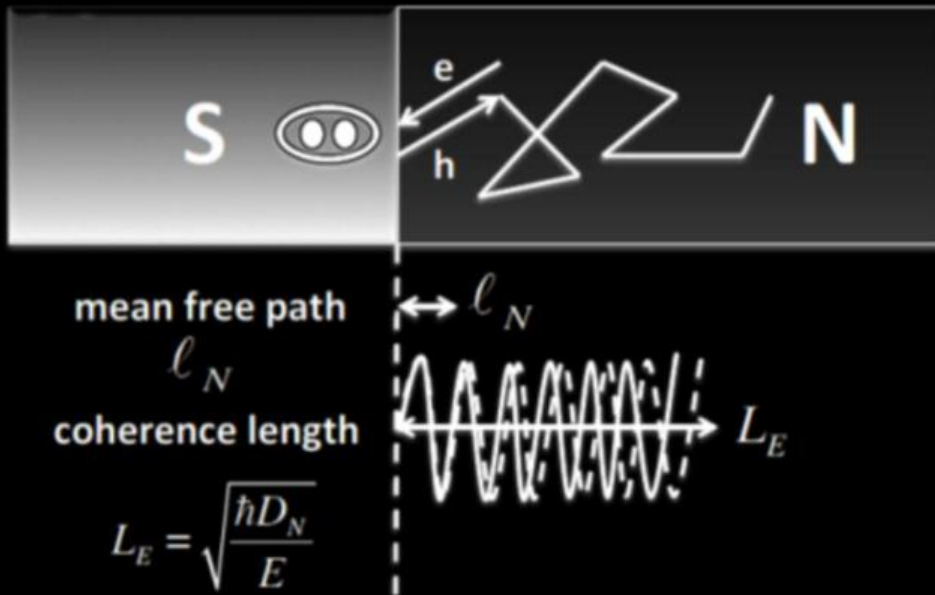
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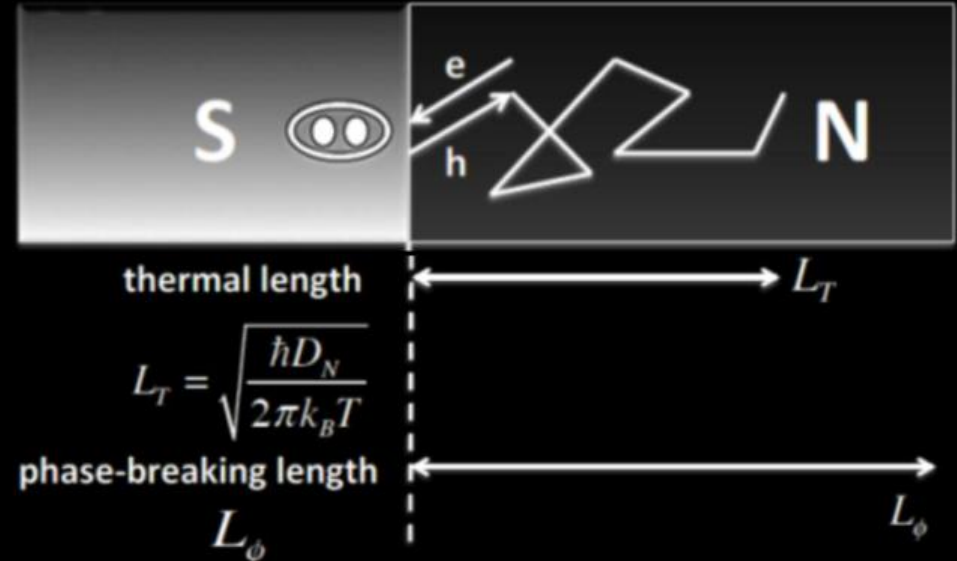
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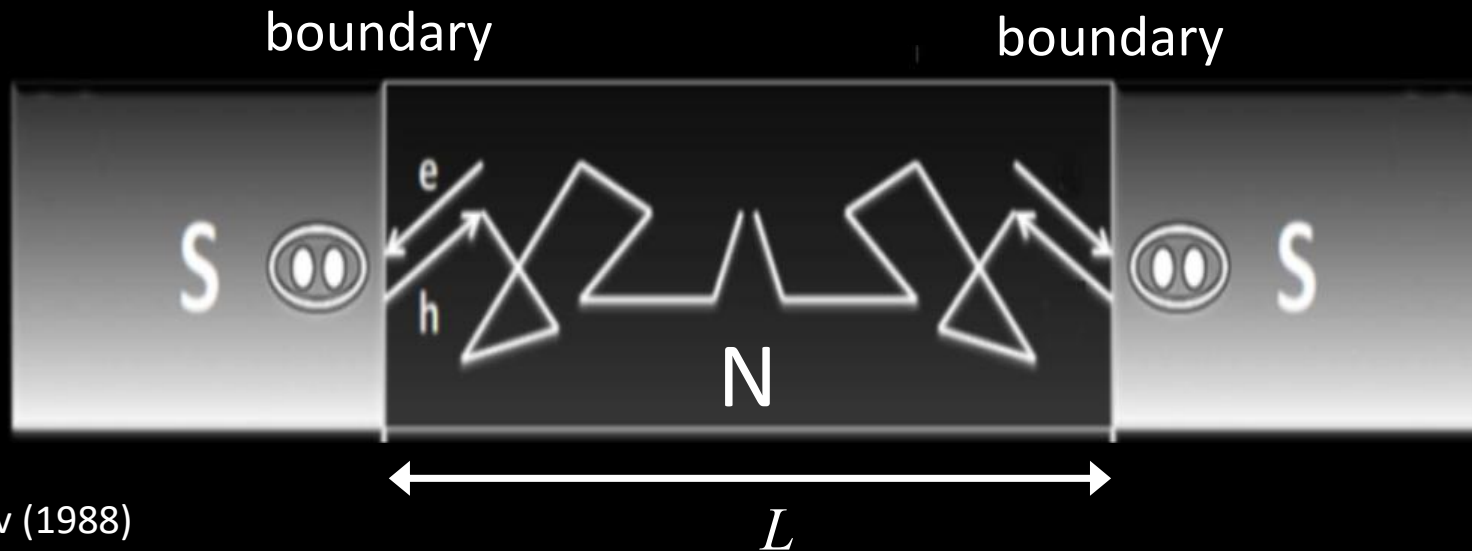
Andreev reflection at the S/N boundary + extended phase coherence in N



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 Zaitsev (1984)



Golubov & Kupriyanov (1988)
 Zhou *et al.* (1998)

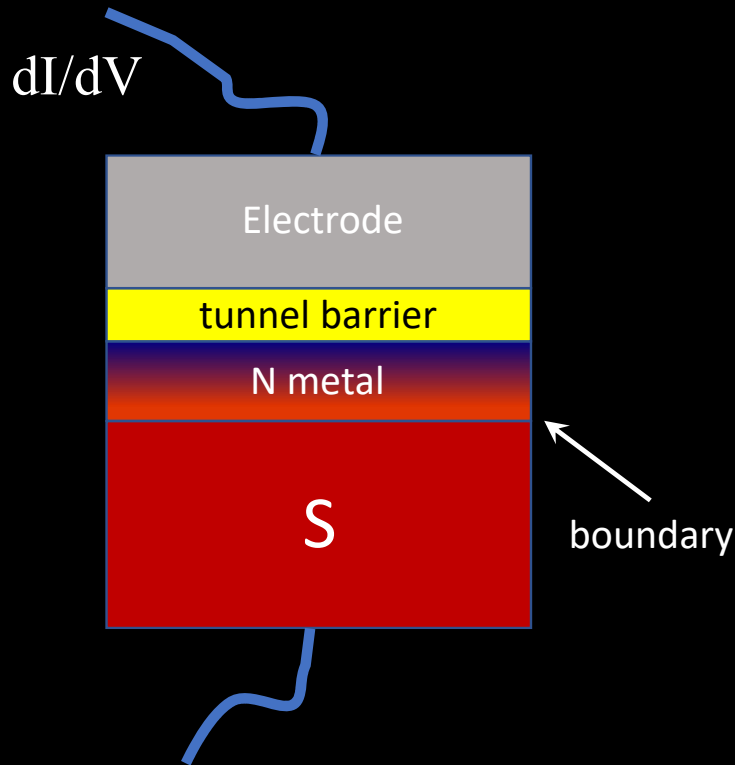
$$L_E > L \Leftrightarrow E < E_{Th} = \hbar D_N / L^2$$

Superconducting correlations propagate for $E < E_{Th}$
 minigap Δ_g connected with E_{Th}

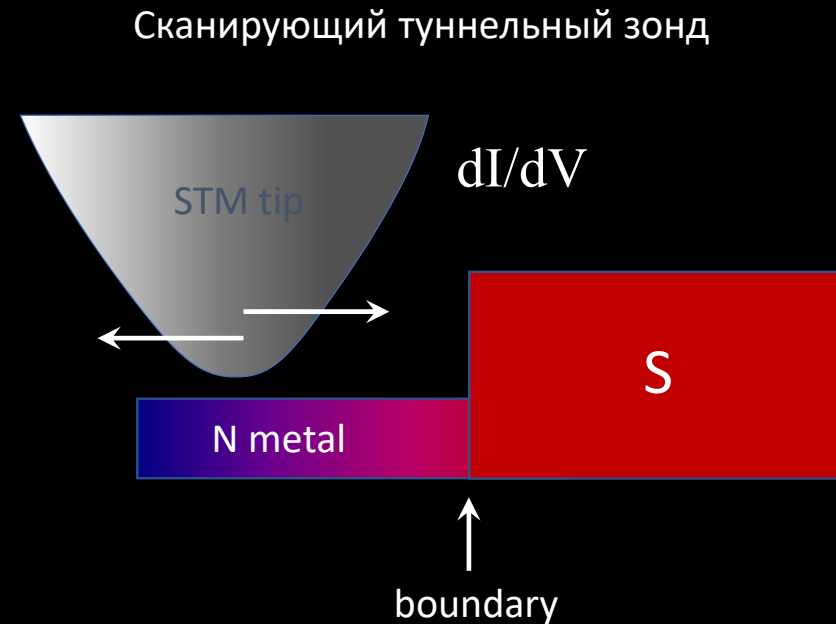
Cryogenic Scanning Tunneling Microscopy

Experiments

Lithographic technologies Fixed tunnel contact



Development: Direct information on the spatial evolution of the density of states





Proximity effect in devises



VOLUME 77, NUMBER 14

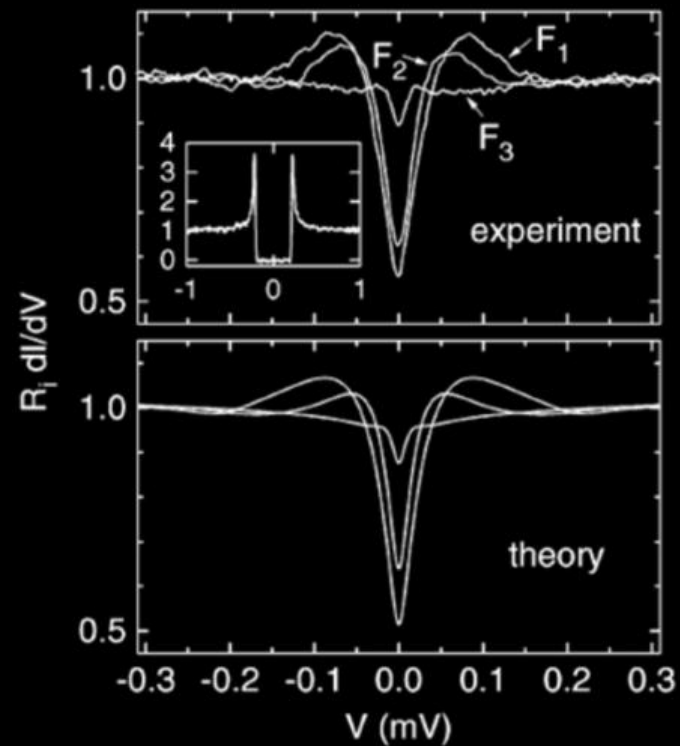
PHYSICAL REVIEW LETTERS

30 SEPTEMBER 1996

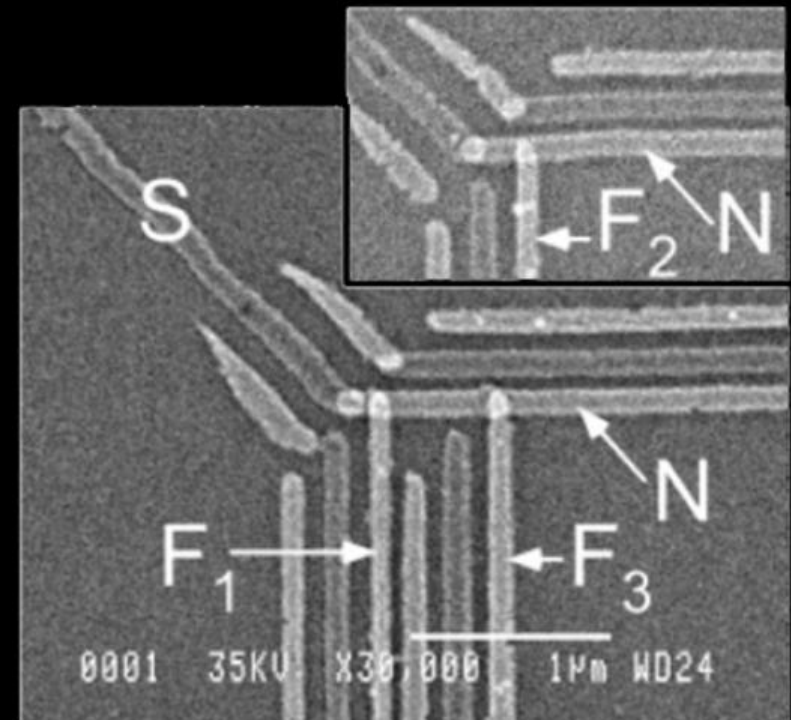
Superconducting Proximity Effect Probed on a Mesoscopic Length Scale

S. Guéron, H. Pothier, Norman O. Birge,* D. Esteve, and M. H. Devoret

Service de Physique de l'Etat Condensé, Commissariat à l'Energie Atomique, Saclay, F-91191 Gif-sur-Yvette Cedex, France
(Received 12 April 1996)



First Study of Spatial Dependency: Nanolithography





Proximity effect in devices



PRL 100, 197002 (2008)

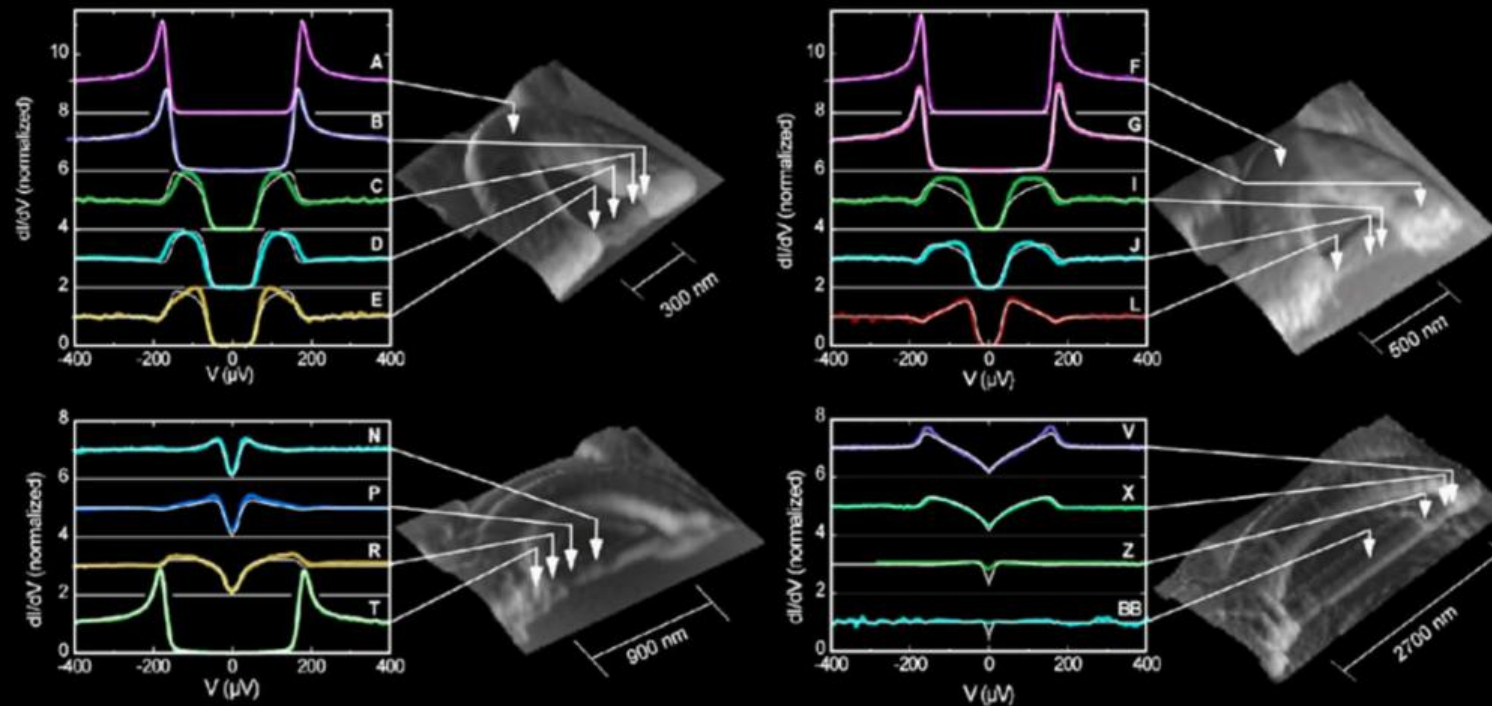
PHYSICAL REVIEW LETTERS

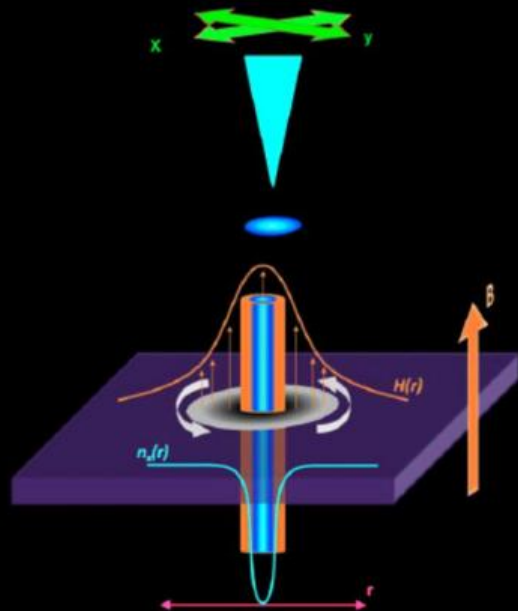
week ending
16 MAY 2008



Phase Controlled Superconducting Proximity Effect Probed by Tunneling Spectroscopy

H. le Sueur, P. Joyez, H. Pothier, C. Urbina, and D. Esteve





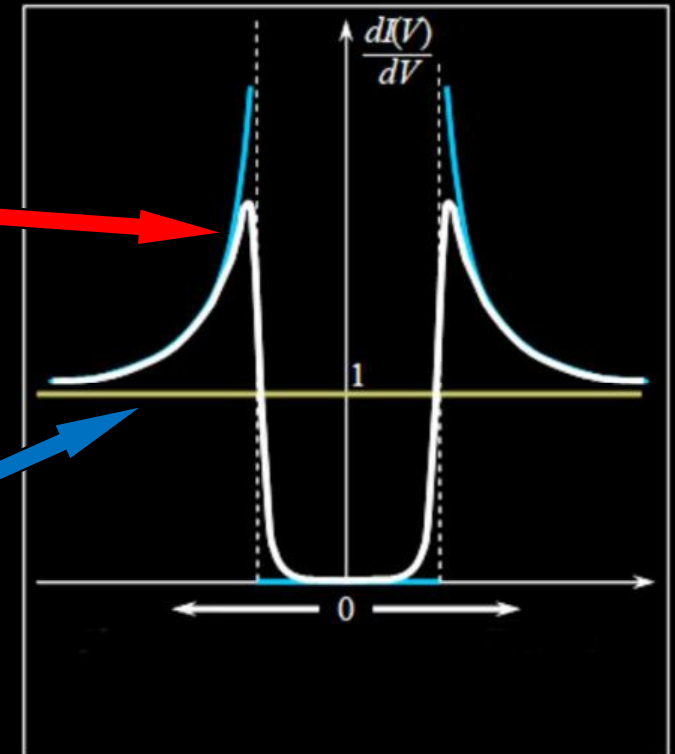
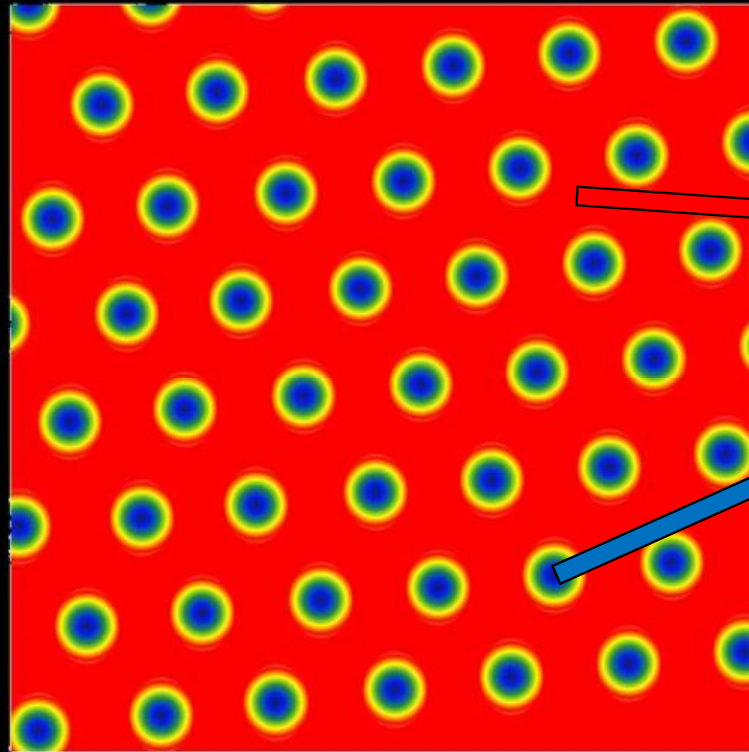
IOP Publishing
 Supercond. Sci. Technol. 27 (2014) 063001 (32pp)
 doi:10.1088/0953-2048/27/6/063001

Topical Review

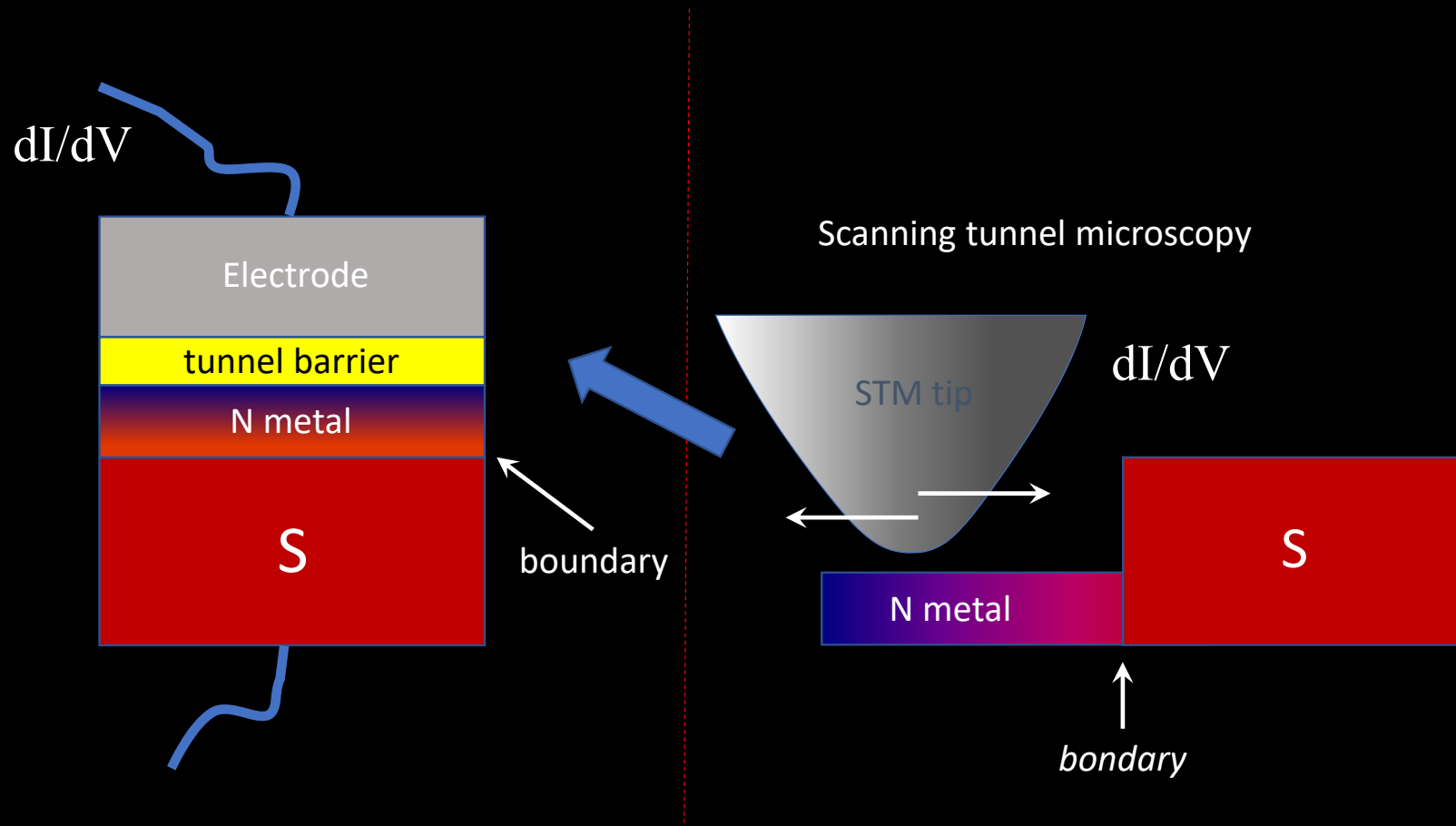
Imaging superconducting vortex cores and lattices with a scanning tunneling microscope

H Suderow^{1,2}, I Guillamón^{1,2,3}, J G Rodrigo^{1,2} and S Vieira^{1,2}

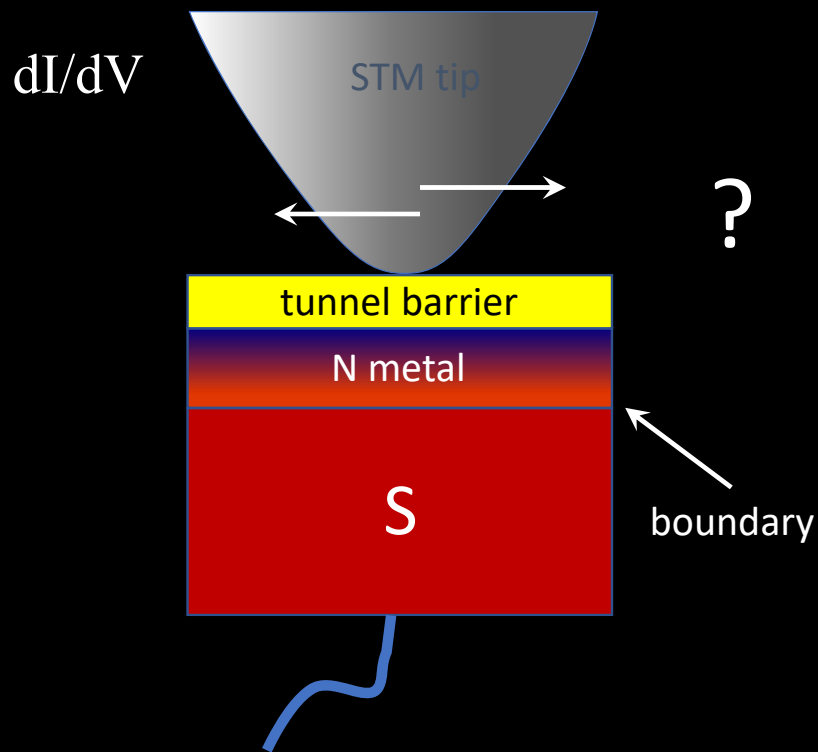
¹ Laboratorio de Bajas Temperaturas, Departamento de Física de la Materia Condensada, Instituto de Ciencia de Materiales Nicolás Cabrera and Condensed Matter Physics Center (IFIMAC), Universidad Autónoma de Madrid, E-28049 Madrid, Spain



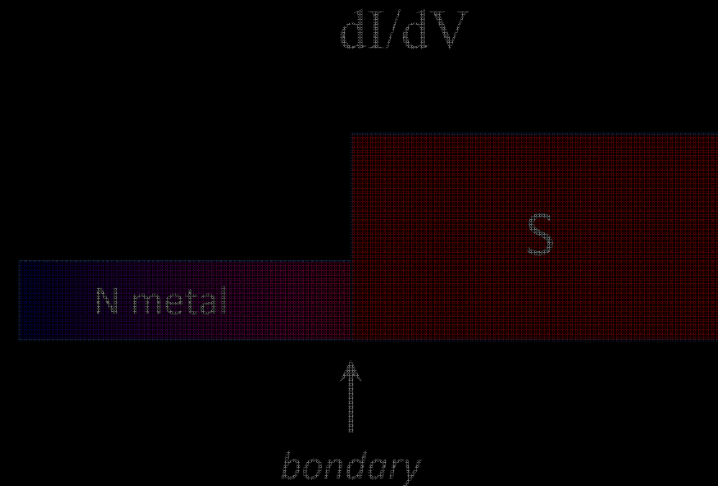
Proximity effect at the boundary of a superconductor with a nonsuperconducting metal in the diffuse limit



Proximity effect at the boundary of a superconductor with a nonsuperconducting metal in the diffuse limit

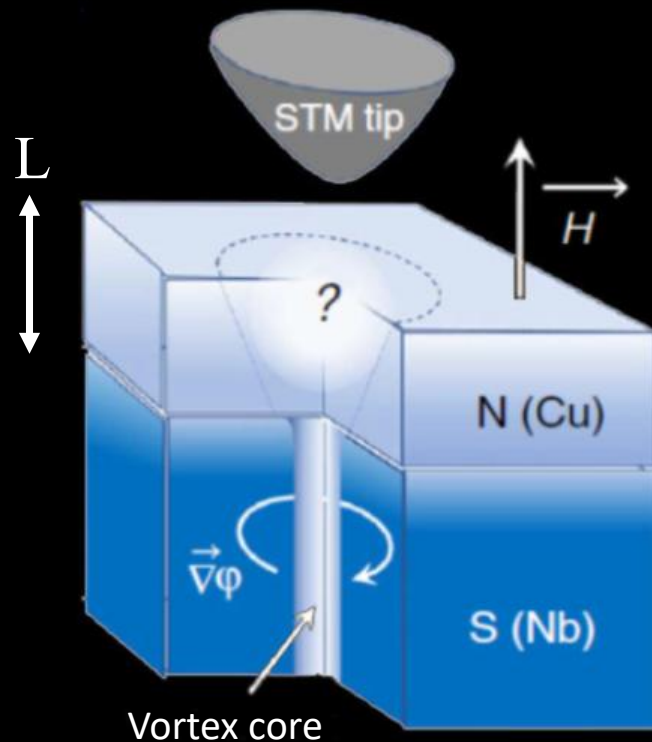


Scanning tunnel microscopy





Proximity effect at the boundary of a superconductor with a nonsuperconducting metal in the diffuse limit



ARTICLE

DOI: 10.1038/s41467-018-04582-1

OPEN



Expansion of a superconducting vortex core into a diffusive metal

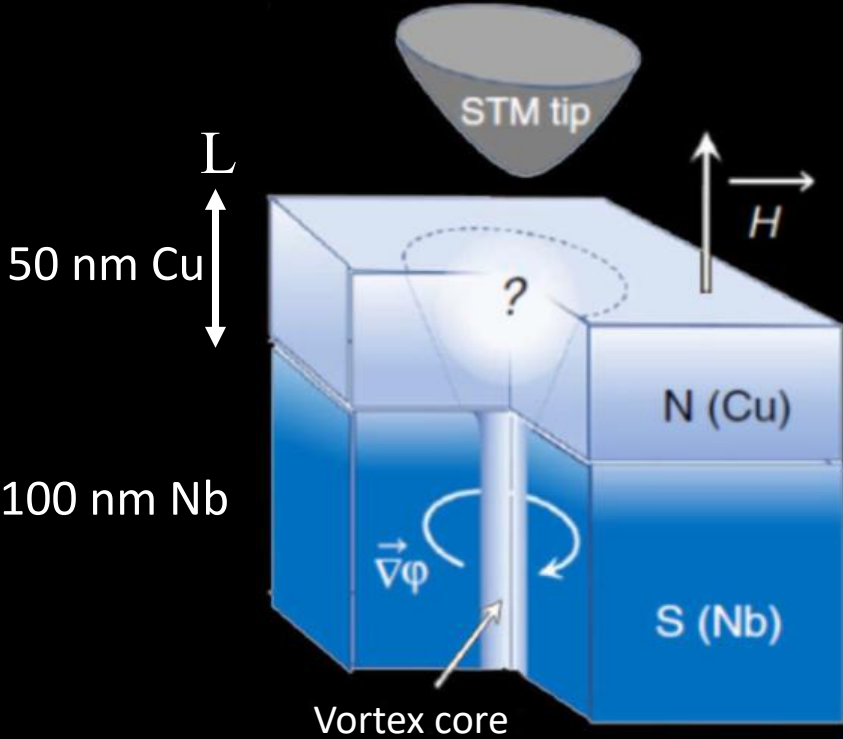
Vasily S. Stolyarov^{1,2,3,4,5}, Tristan Cren², Christophe Brun², Igor A. Golovchanskiy^{1,5}, Olga V. Skryabina^{1,3}, Daniil I. Kasatonov¹, Mikhail M. Khapaev^{1,6,7}, Mikhail Yu. Kupriyanov^{1,7,8}, Alexander A. Golubov^{1,9} & Dimitri Roditchev^{1,2,10,11}

Vortex size?

3D- proximity effect

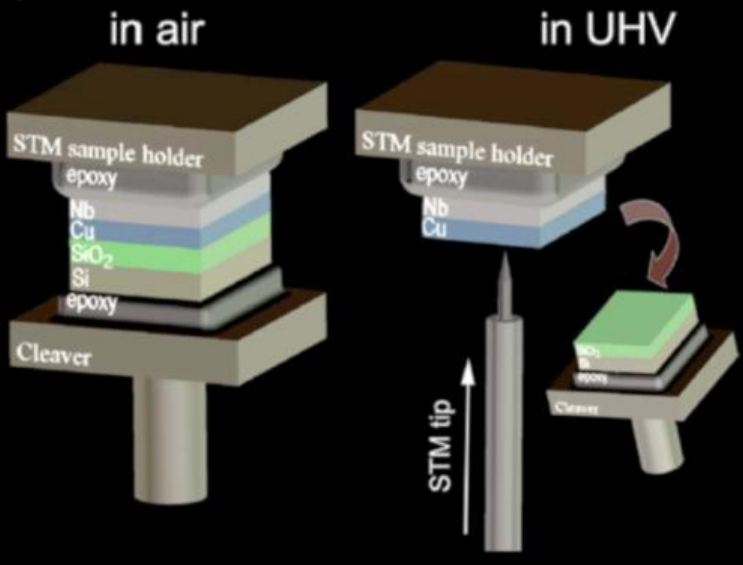
minigap Δ , related to $\hbar D_N / L^2$

Proximity effect at the boundary of a superconductor with a nonsuperconducting metal in the diffuse limit



Cu, Nb:
Magnetron sputtering

- $d_{Nb} = 100 \text{ nm}$
- $d_{Cu} = 50 \text{ nm}$
- $d_{SiO_2} = 270 \text{ nm}$
- $d_{Si} = 0.3 \text{ mm}$



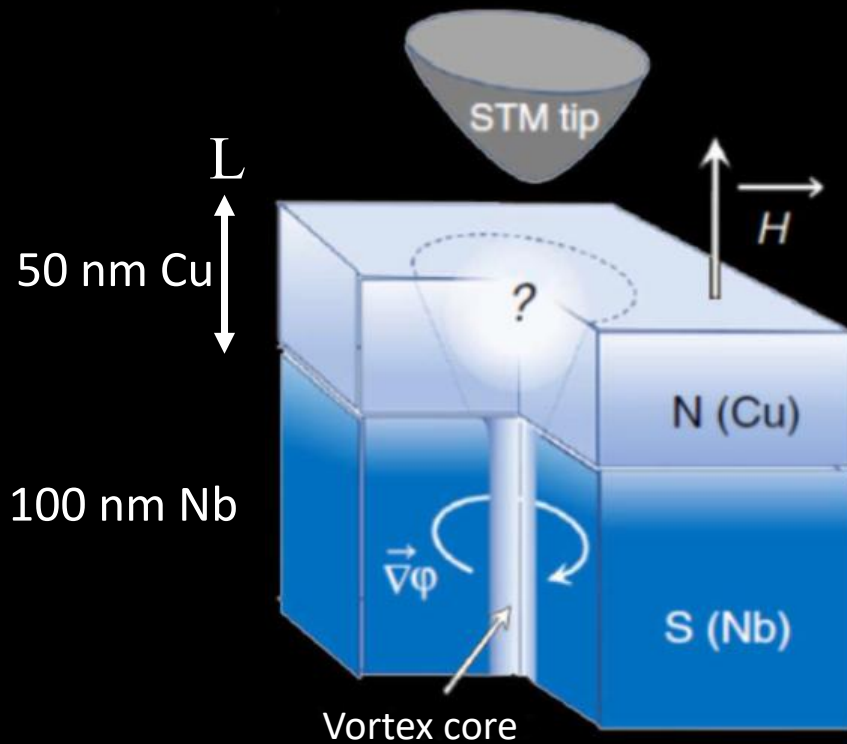
APPLIED PHYSICS LETTERS 104, 172604 (2014)



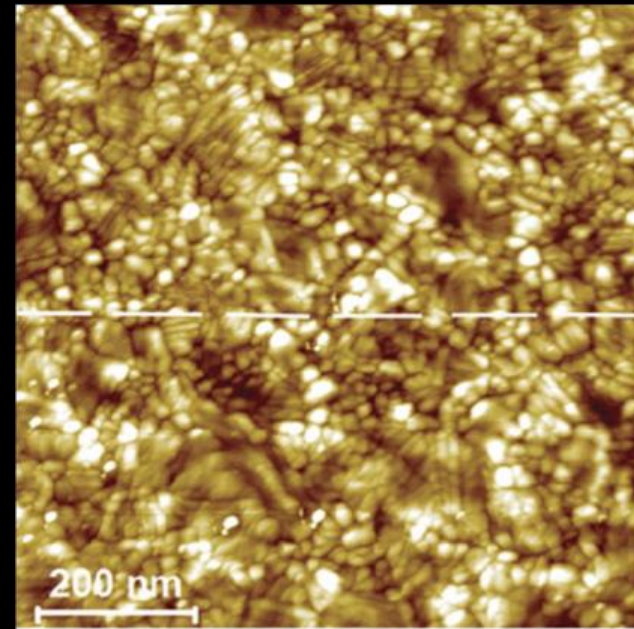
Ex situ elaborated proximity mesoscopic structures for ultrahigh vacuum scanning tunneling spectroscopy

V. S. Stolyarov,^{1,2,3,4,5,6} T. Cren,^{1,2,a)} F. Debontridder,^{1,2} C. Brun,^{1,2} I. S. Veshchunov,^{7,3}
 O. V. Skryabina,³ A. Yu. Rusanov,⁸ and D. Roditchev^{1,2,9}
¹UMR 7588, Institut des Nanosciences de Paris, UPMC Univ Paris 06, Sorbonne Universités, F-75005 Paris, France

Proximity effect at the boundary of a superconductor with a nonsuperconducting metal in the diffuse limit



STM topography

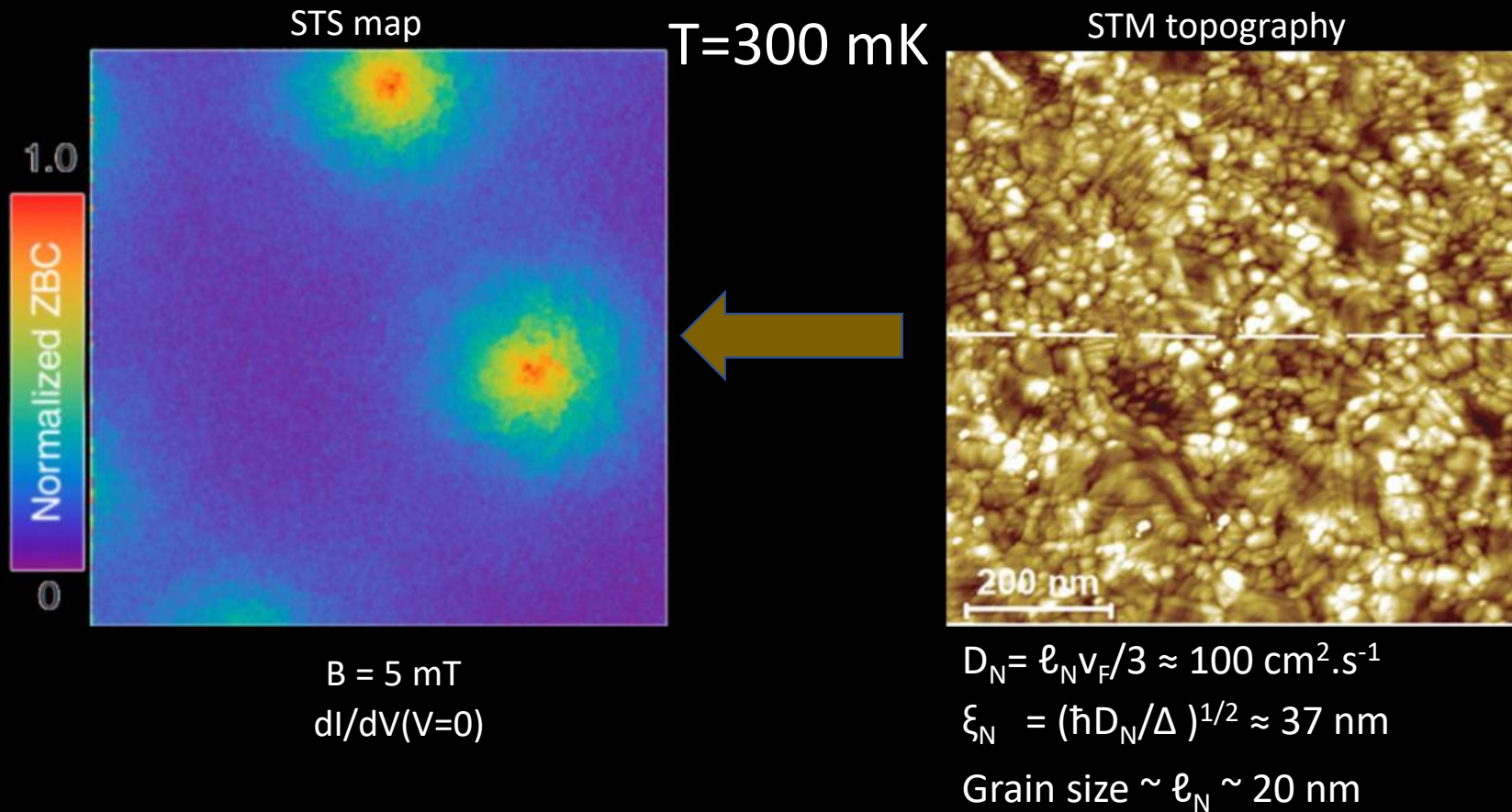


$$D_N = \ell_N v_F / 3 \approx 100 \text{ cm}^2 \cdot \text{s}^{-1}$$

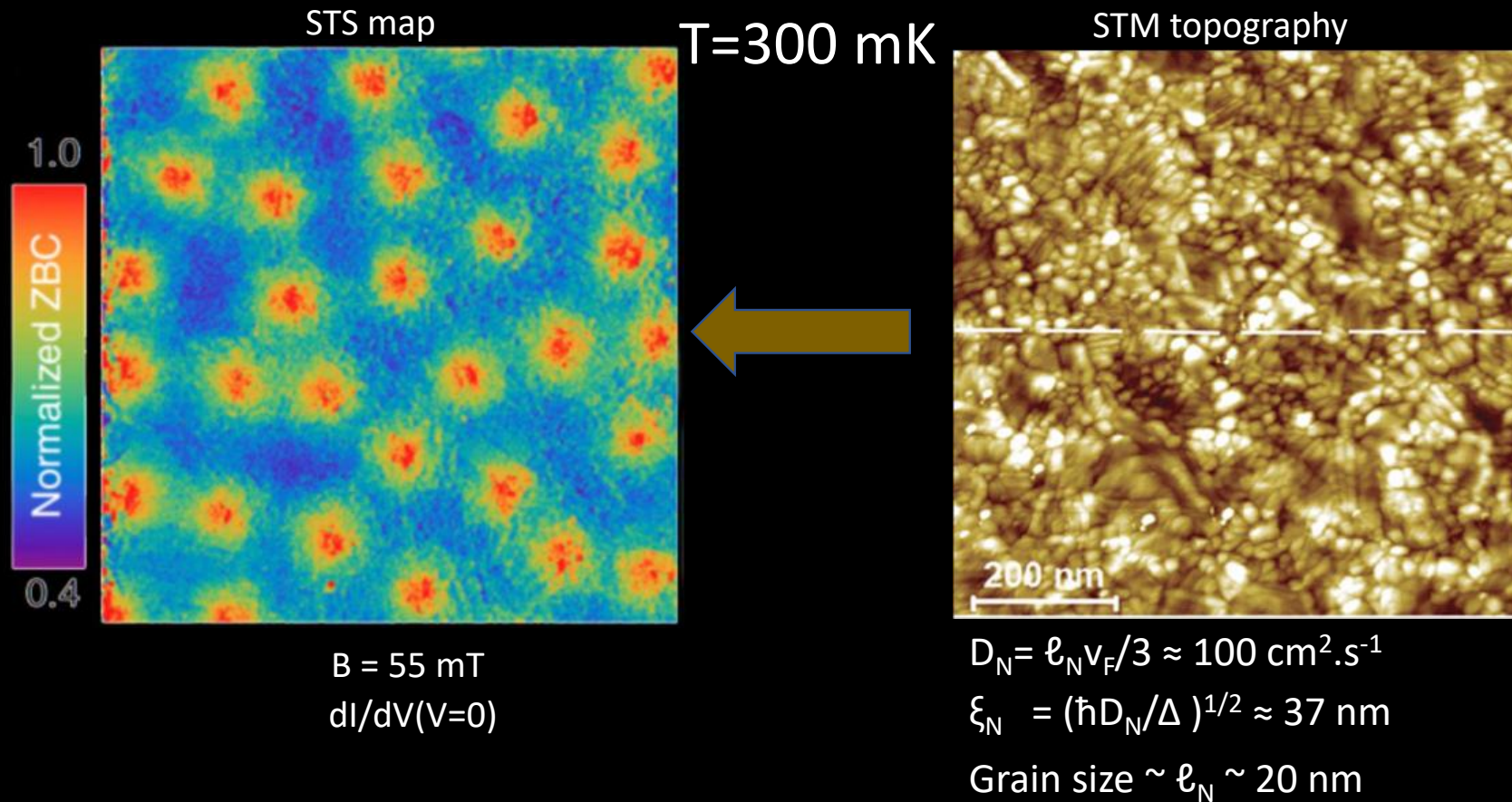
$$\xi_N = (\hbar D_N / \Delta)^{1/2} \approx 37 \text{ nm}$$

Grain size $\sim \ell_N \sim 20 \text{ nm}$

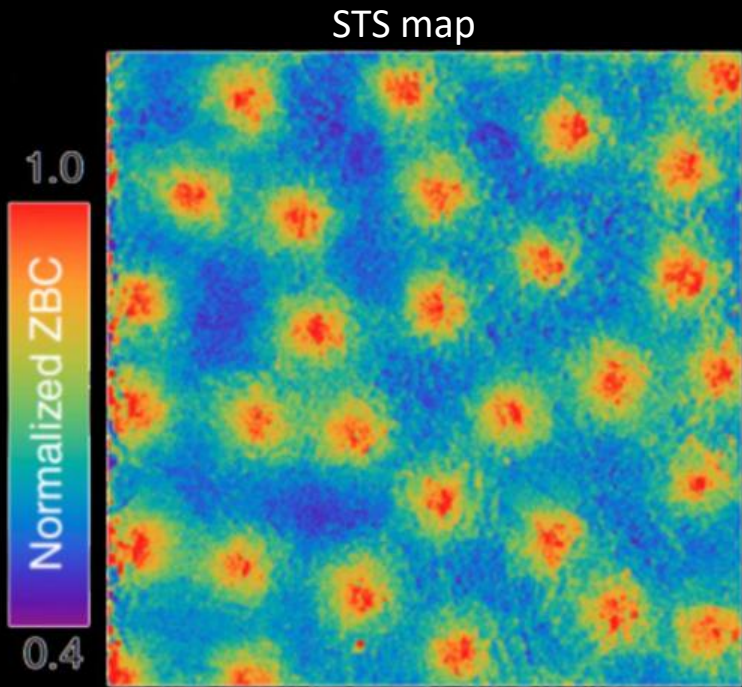
Proximity effect at the boundary of a superconductor with a nonsuperconducting metal in the diffuse limit



Proximity effect at the boundary of a superconductor with a nonsuperconducting metal in the diffuse limit

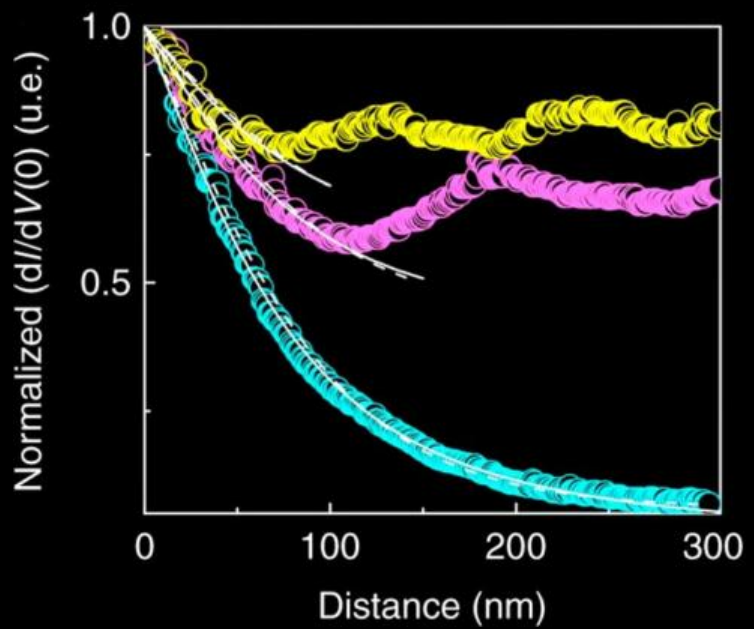


Proximity effect at the boundary of a superconductor with a nonsuperconducting metal in the diffuse limit



T=300 mK

B = 55 mT
 $dI/dV(V=0)$



$$D_N = \ell_N v_F / 3 \approx 100 \text{ cm}^2 \cdot \text{s}^{-1}$$

$$\xi_N = (\hbar D_N / \Delta)^{1/2} \approx 37 \text{ nm}$$

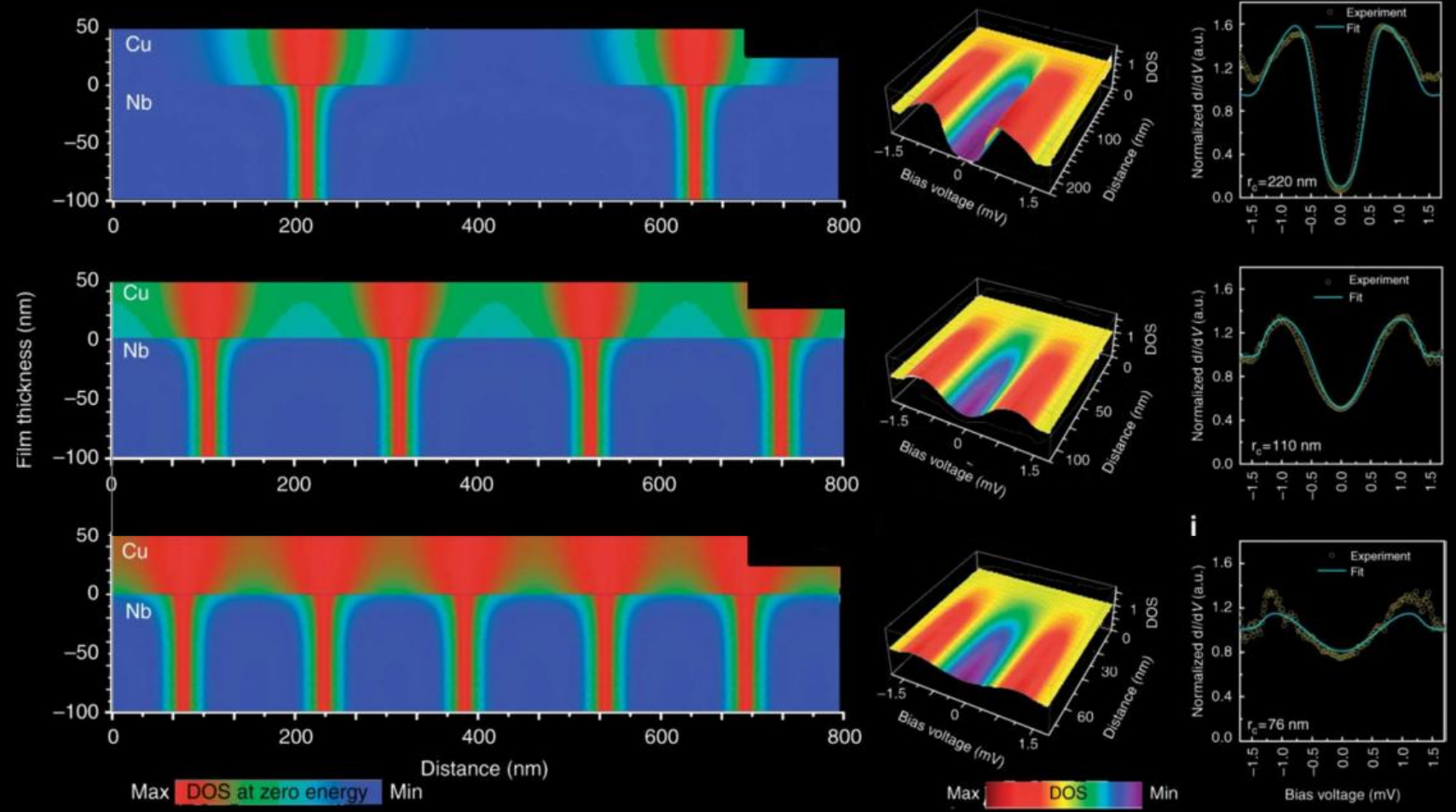
Grain size $\sim \ell_N \sim 20 \text{ nm}$



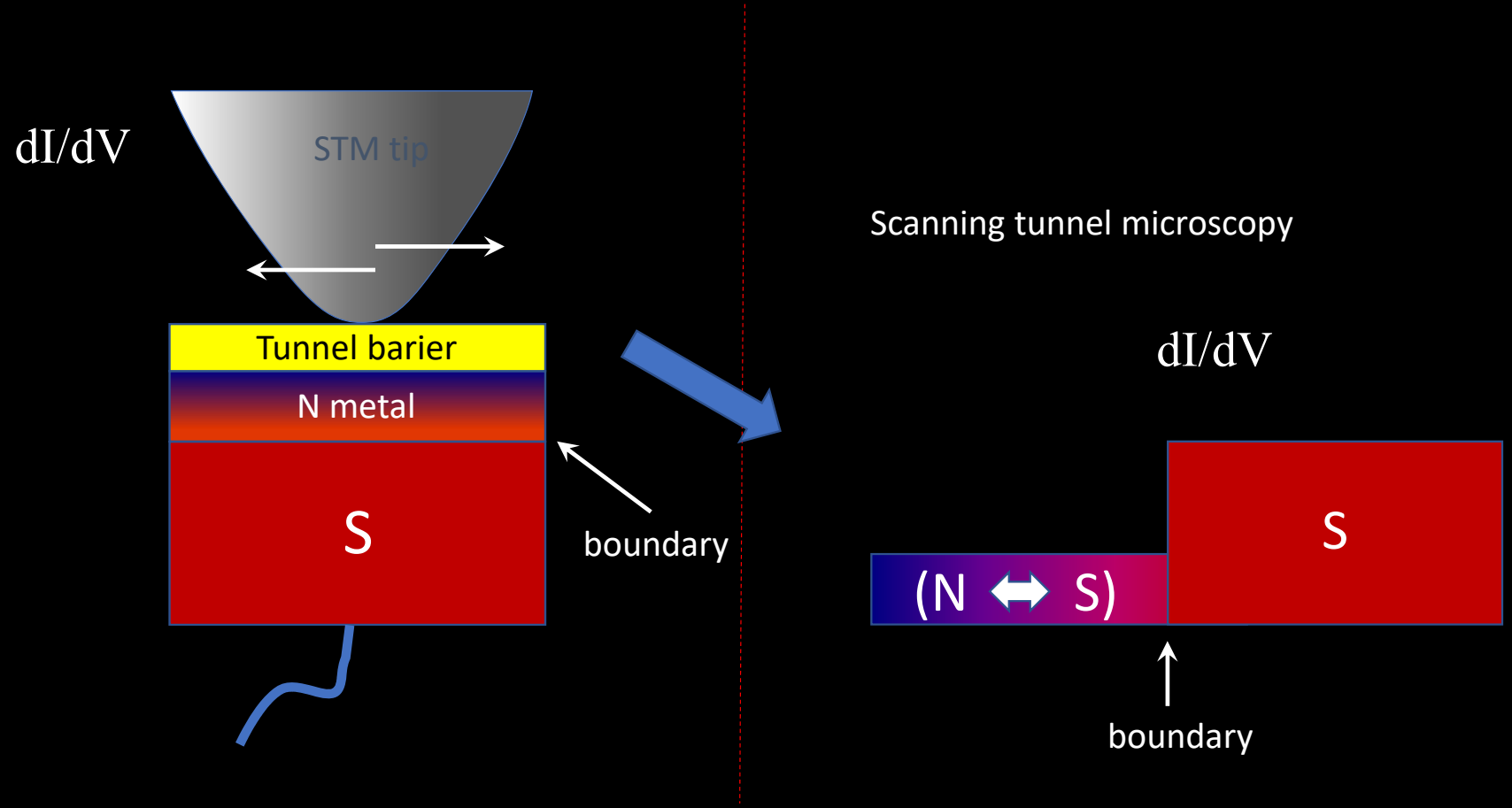
Proximity effect at the boundary of a superconductor with a nonsuperconducting metal in the diffuse limit



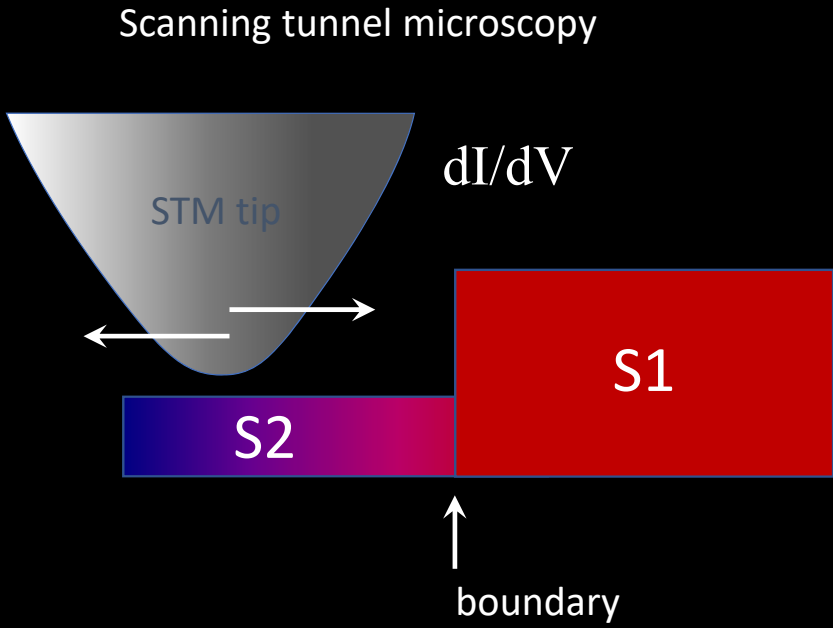
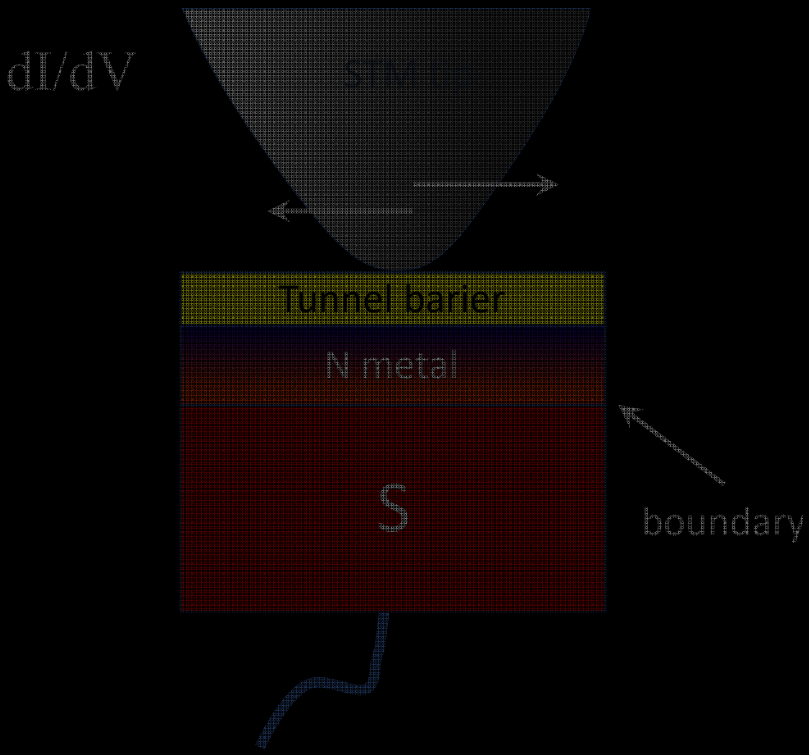
$R_b = 150 \text{ Ohm}$



Proximity effect between two superconductors



Proximity effect between two superconductors



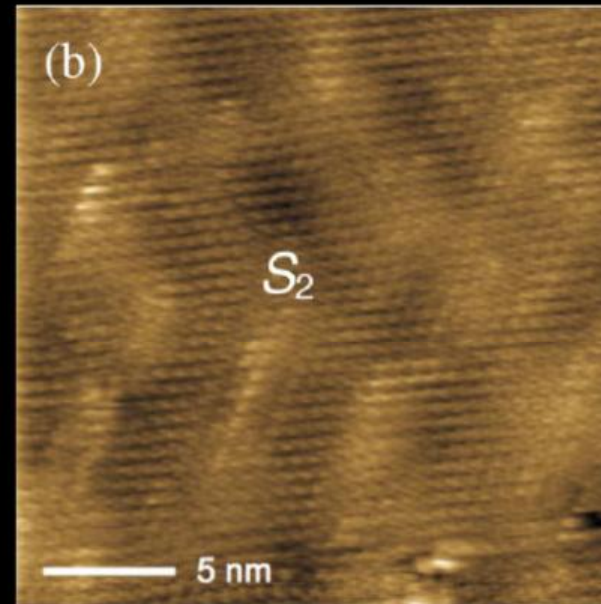
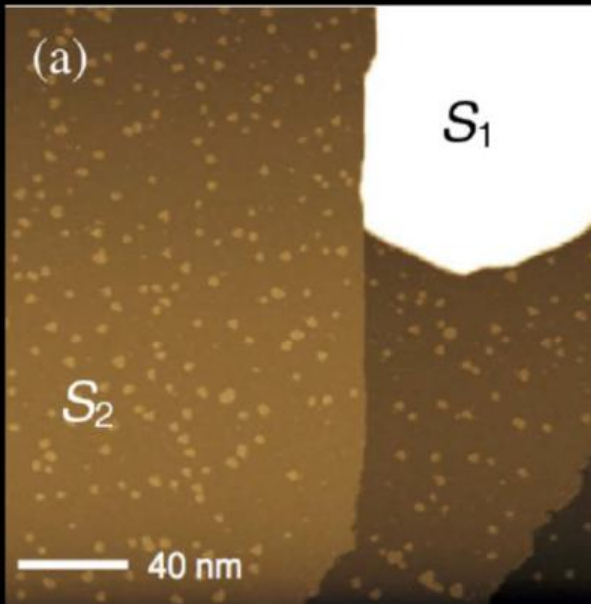
Proximity effect between two superconductors

PHYSICAL REVIEW X 4, 011033 (2014)

Proximity Effect between Two Superconductors Spatially Resolved by Scanning Tunneling Spectroscopy

V. Cherkez,^{1,2} J. C. Cuevas,^{3,*} C. Brun,^{1,2,†} T. Cren,^{1,2} G. Ménard,^{1,2} F. Debontridder,^{1,2}
V. S. Stolyarov,^{1,2,5,6} and D. Roditchev^{1,4}

¹Institut des Nanosciences de Paris, Sorbonne Universités, UPMC Université Paris 06, UMR 7588, F-75005 Paris, France



$$\Delta_1 = 1.2 \text{ mB} \quad \Delta_2 = 0.23 \text{ mB}$$

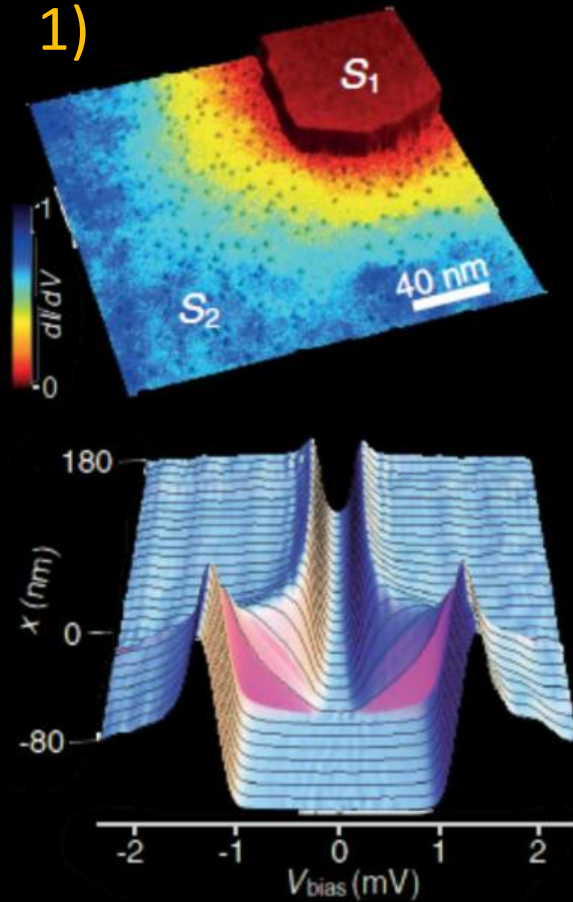
$$T_{C1} = 6.2 \text{ K}, \quad T_{C2} = 1.8 \text{ K}$$

$$T = 0.3 \text{ K} < T_{C1}, T_{C2}$$

фаза $\sqrt{7} \times \sqrt{3}$ -Pb/Si(111)

Proximity effect between two superconductors

1)



PHYSICAL REVIEW X 4, 011033 (2014)

Proximity Effect between Two Superconductors Spatially Resolved by Scanning Tunneling Spectroscopy

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V. S. Stolyarov,^{1,2,5,6} and D. Roditchev^{1,4}

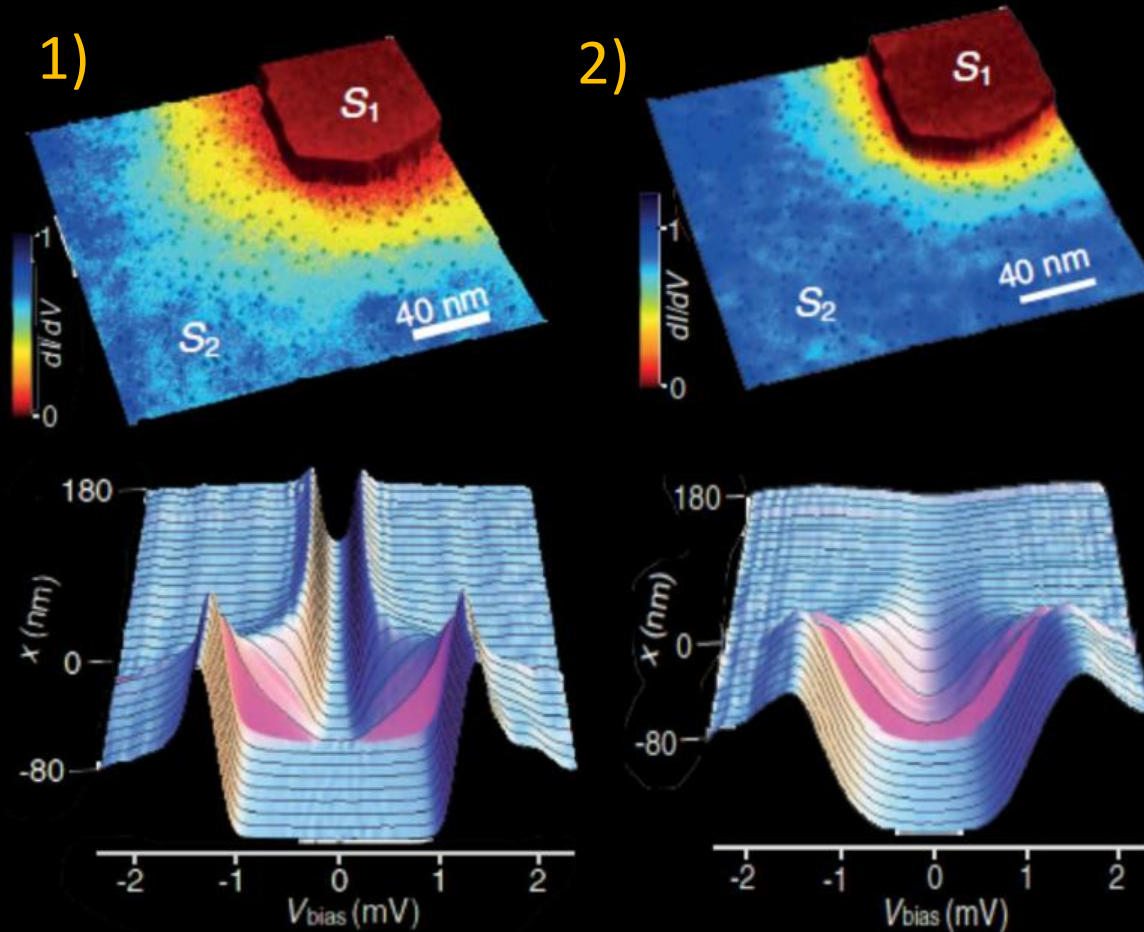
¹Institut des Nanosciences de Paris, Sorbonne Universités, UPMC Université Paris 06, UMR 7588, F-75005 Paris, France

$$\Delta_1 = 1.2 \text{ mB} \quad \Delta_2 = 0.23 \text{ mB}$$

$$T_{C1} = 6.2 \text{ K}, \quad T_{C2} = 1.8 \text{ K}$$

$$1) T = 0.3 \text{ K} < T_{C1}, T_{C2}$$

Proximity effect between two superconductors



PHYSICAL REVIEW X 4, 011033 (2014)

Proximity Effect between Two Superconductors Spatially Resolved by Scanning Tunneling Spectroscopy

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¹Institut des Nanosciences de Paris, Sorbonne Universités, UPMC Université Paris 06, UMR 7588, F-75005 Paris, France

$$\Delta_1 = 1.2 \text{ mB} \quad \Delta_2 = 0.23 \text{ mB}$$

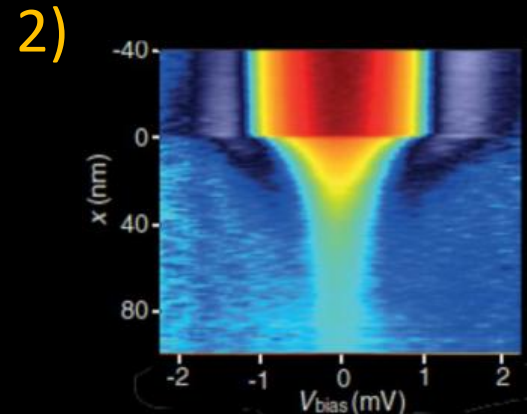
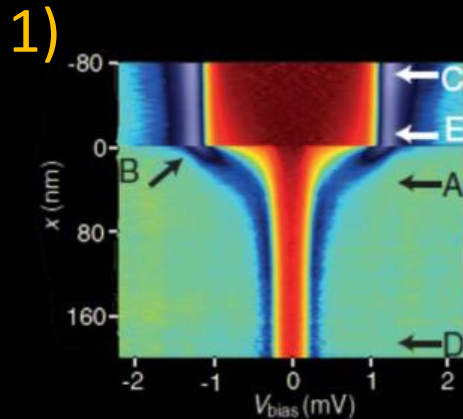
$$T_{C1} = 6.2 \text{ K}, \quad T_{C2} = 1.8 \text{ K}$$

$$1) \quad T = 0.3 \text{ K} < T_{C1}, T_{C2}$$

$$2) \quad T_{C2} < T = 2.05 \text{ K} < T_{C1}$$

Proximity effect between two superconductors

PHYSICAL REVIEW X 4, 011033 (2014)



Proximity Effect between Two Superconductors Spatially Resolved by Scanning Tunneling Spectroscopy

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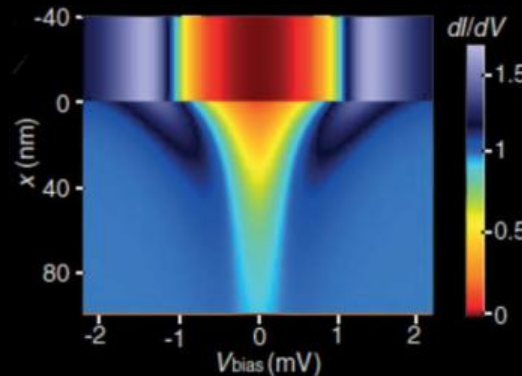
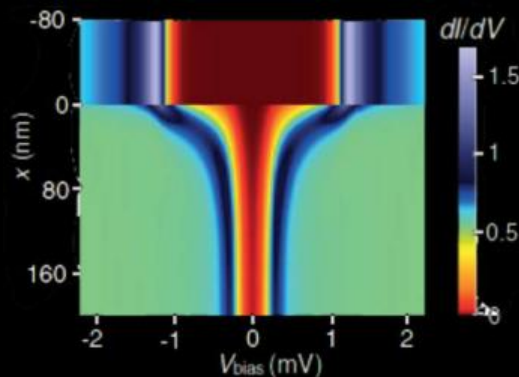
¹Institut des Nanosciences de Paris, Sorbonne Universités, UPMC Université Paris 06, UMR 7588, F-75005 Paris, France

$$\Delta_1 = 1.2 \text{ mB} \quad \Delta_2 = 0.23 \text{ mB}$$

$$T_{C1} = 6.2 \text{ K}, \quad T_{C2} = 1.8 \text{ K}$$

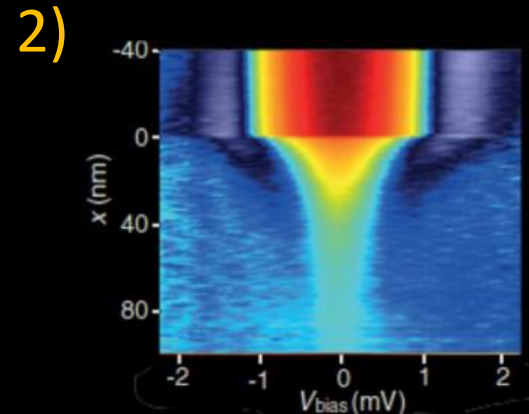
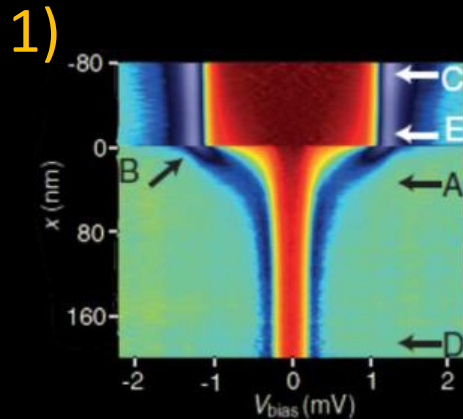
$$1) \quad T = 0.3 \text{ K} < T_{C1}, T_{C2}$$

$$2) \quad T_{C2} < T = 2.05 \text{ K} < T_{C1}$$



Proximity effect between two superconductors

PHYSICAL REVIEW X 4, 011033 (2014)



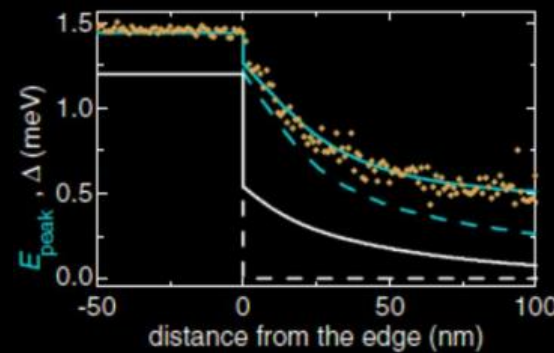
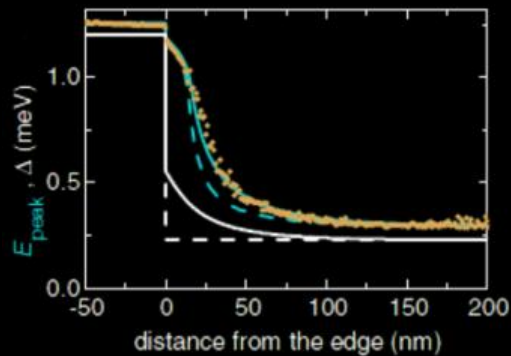
Proximity Effect between Two Superconductors Spatially Resolved by Scanning Tunneling Spectroscopy

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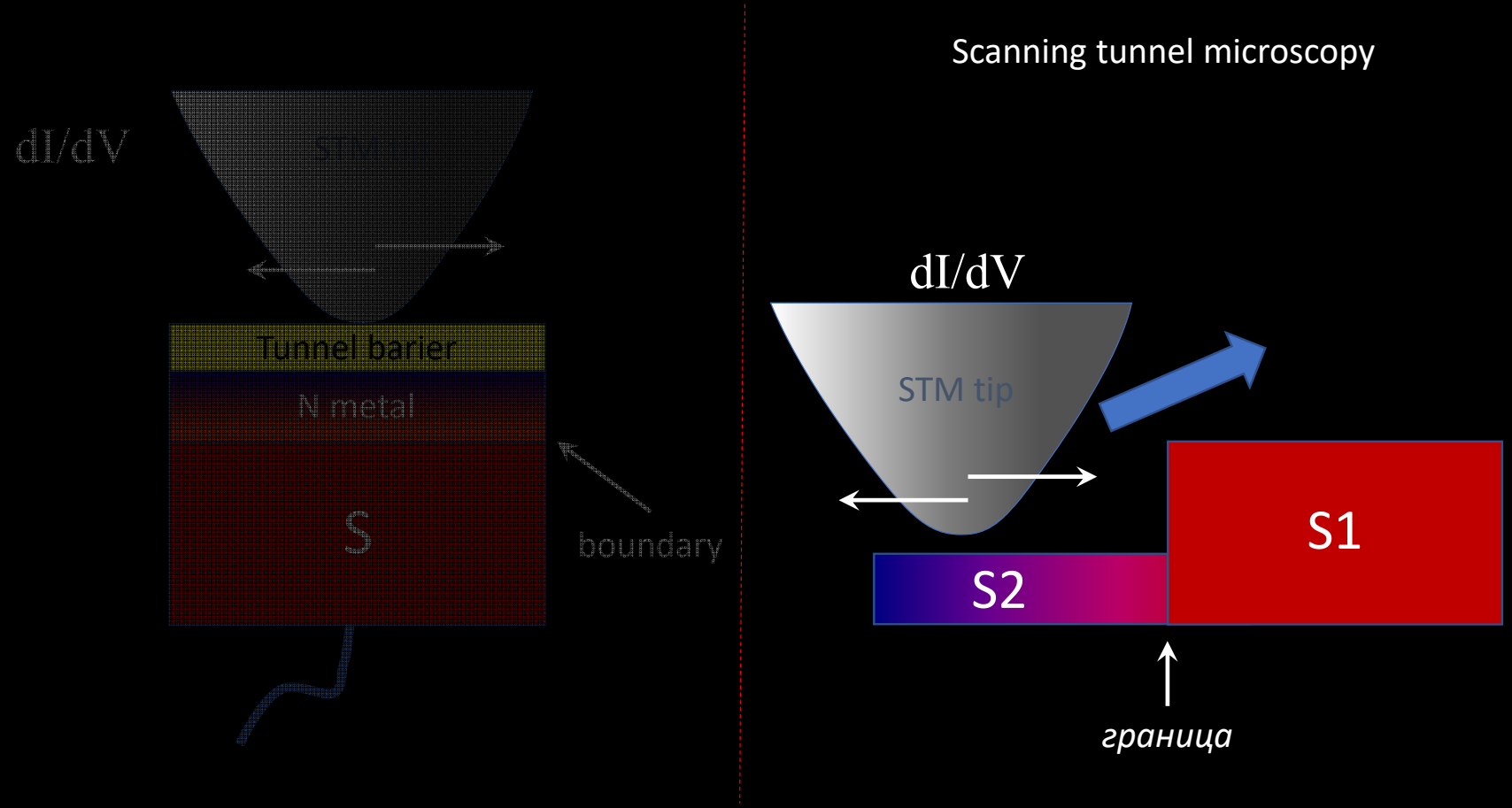


1) $T = 0.3 \text{ K} < T_{C1}, T_{C2}$

2) $T_{C2} < T = 2.05 \text{ K} < T_{C1}$

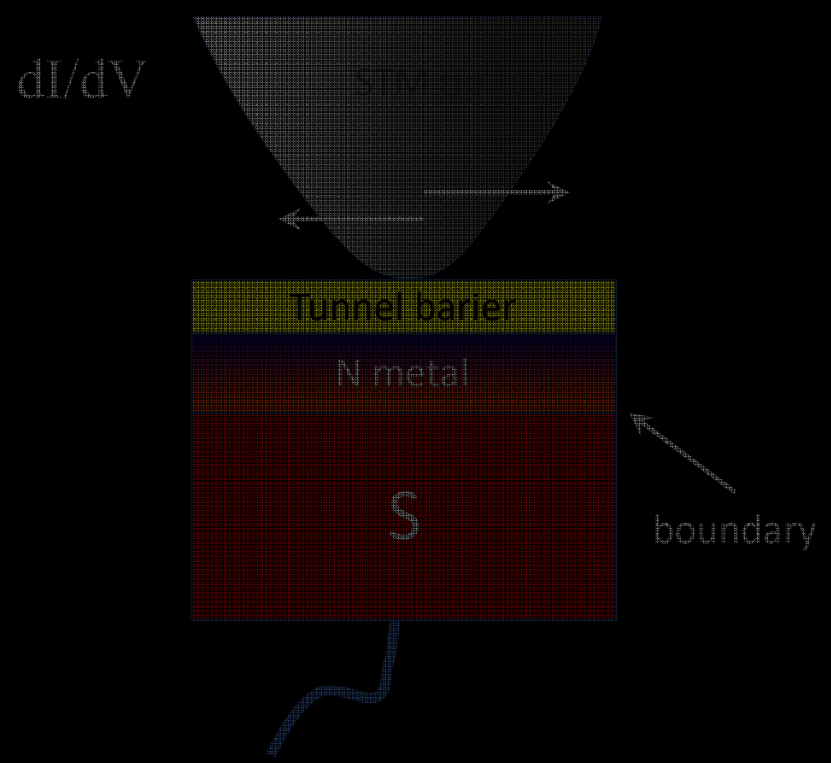


Proximity effect in a superconductor in the ballistic limit

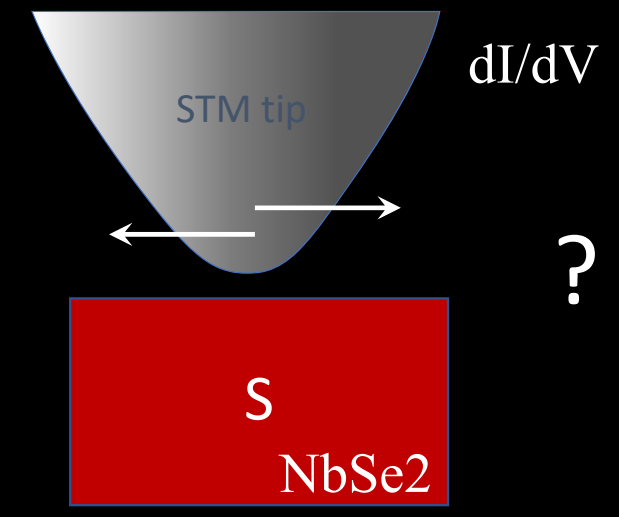




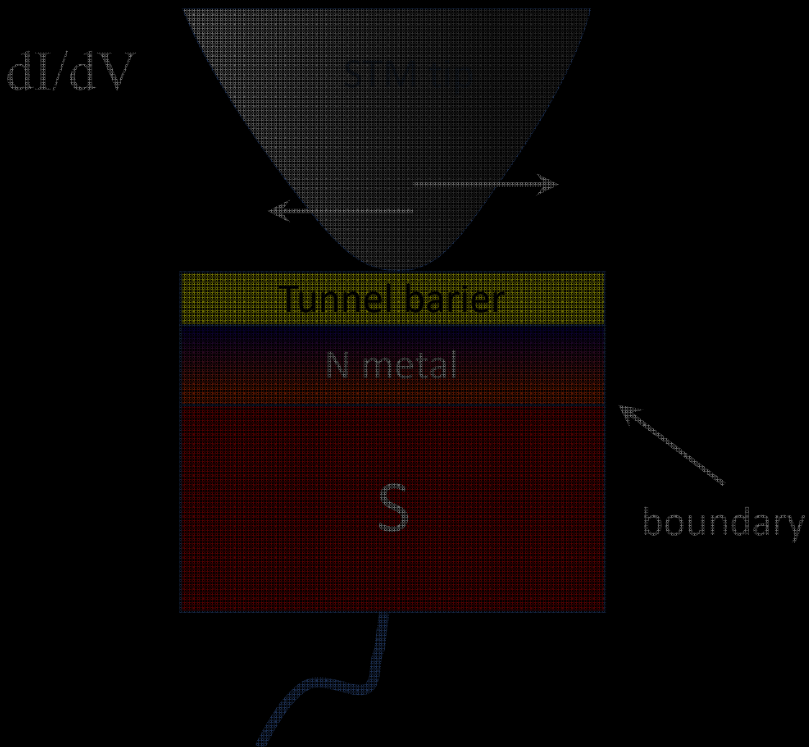
Proximity effect in a superconductor in the ballistic limit



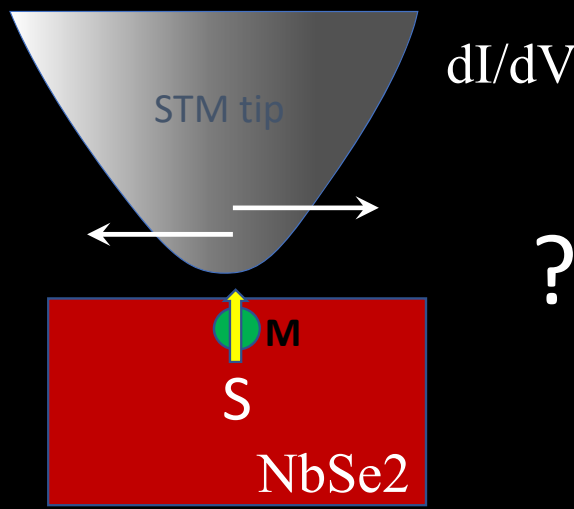
Scanning tunnel microscopy



Proximity effect in a superconductor in the ballistic limit



Scanning tunnel microscopy



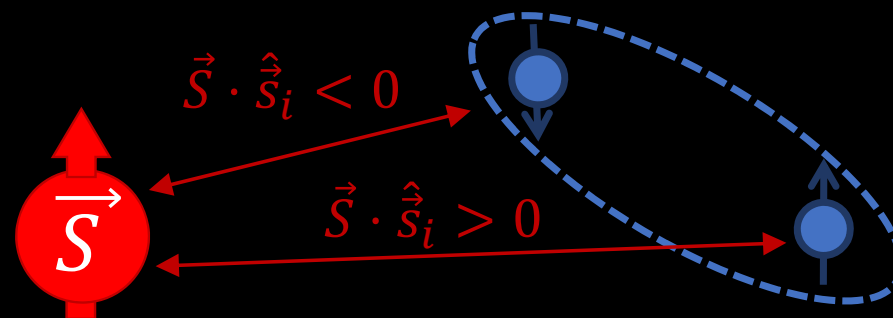
Long-range Shiba bound states

Yu-Shiba-Rusinov (YSR) problem:
3D scattering on a classical spin \vec{S}

L. Yu. Acta Phys. Sin (1965)

H. Shiba. Prog. Th. Phys. (1968)

A. I. Rusinov JETP Lett. (1969)



Two terms hamiltonian: magnetic and non-magnetic scattering

$$H_{Imp} = -\frac{JS}{2}(c_{0\uparrow}^\dagger c_{0\uparrow} - c_{0\downarrow}^\dagger c_{0\downarrow}) + K(c_{0\uparrow}^\dagger c_{0\uparrow} + c_{0\downarrow}^\dagger c_{0\downarrow})$$

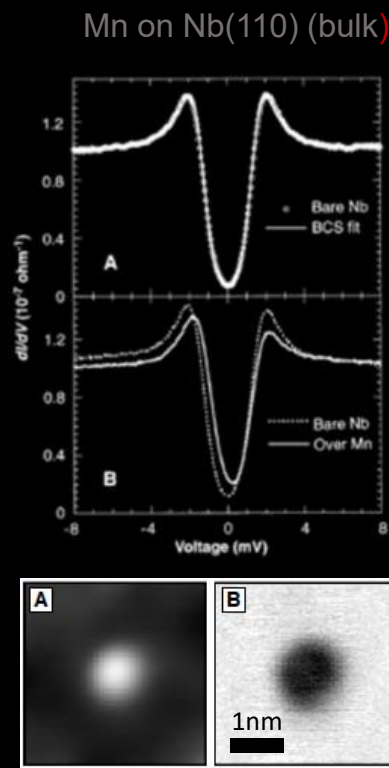
$$E_{Shiba} = \pm\Delta \cos(\delta^+ - \delta^-) \quad \text{where} \quad \tan \delta^\pm = K\nu_0 \pm \frac{JS}{2}\nu_0$$

$$\psi_\pm(r) = \frac{1}{\sqrt{N}} \frac{\sin(k_F r + \delta^\pm)}{k_F r} e^{-\Delta \sin(\delta^+ - \delta^-) r / \hbar v_F}$$

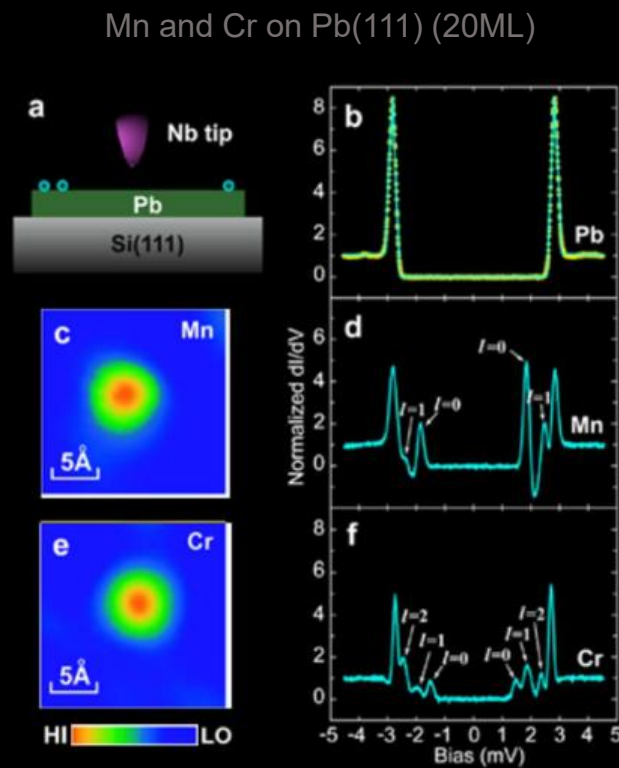
$$\frac{\Delta}{\hbar v_F} \approx \xi^{-1}$$

valid for $k_F r \gg 1$

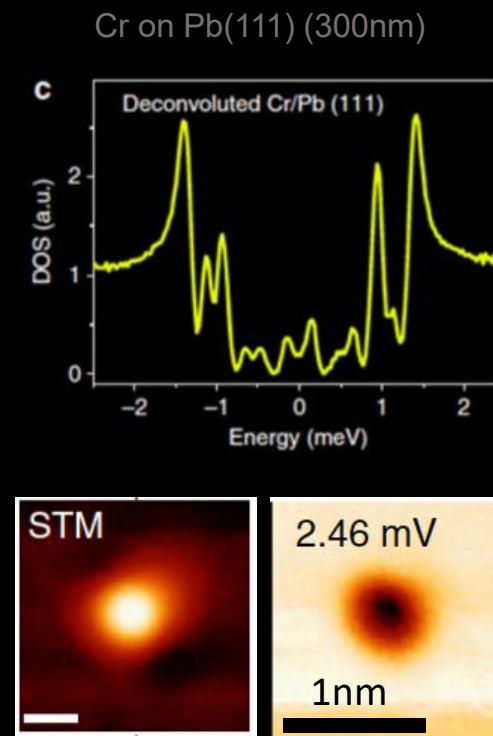
Long-range Shiba bound states



A. Yazdani et al. *Science* (1997)



Shuai-Hua Ji, *PRL* (2008)

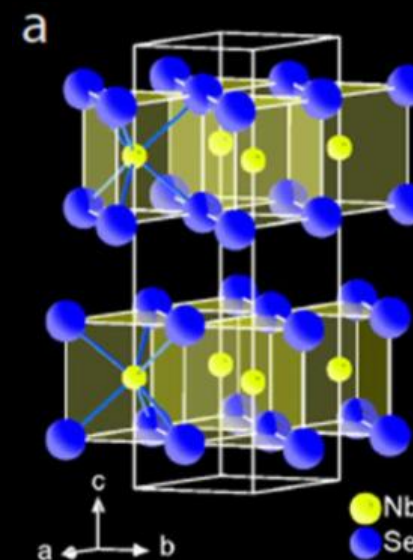
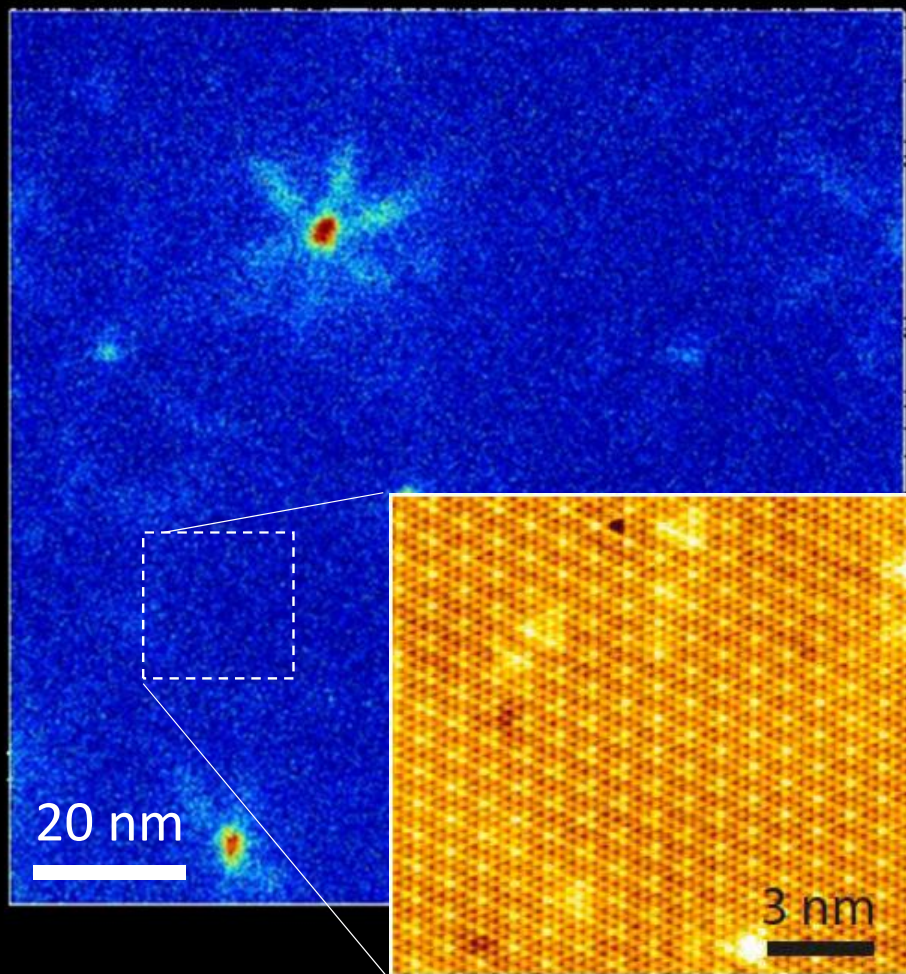


D.-J. Choi et al. *Nat. Comm.* (2017)

$$\psi_{\pm}(r) = \frac{1}{\sqrt{N}} \frac{\sin(k_F r + \delta^{\pm})}{k_F r} e^{-\Delta \sin(\delta^+ - \delta^-) r / \hbar v_F}$$

valid for $k_F r \gg 1$

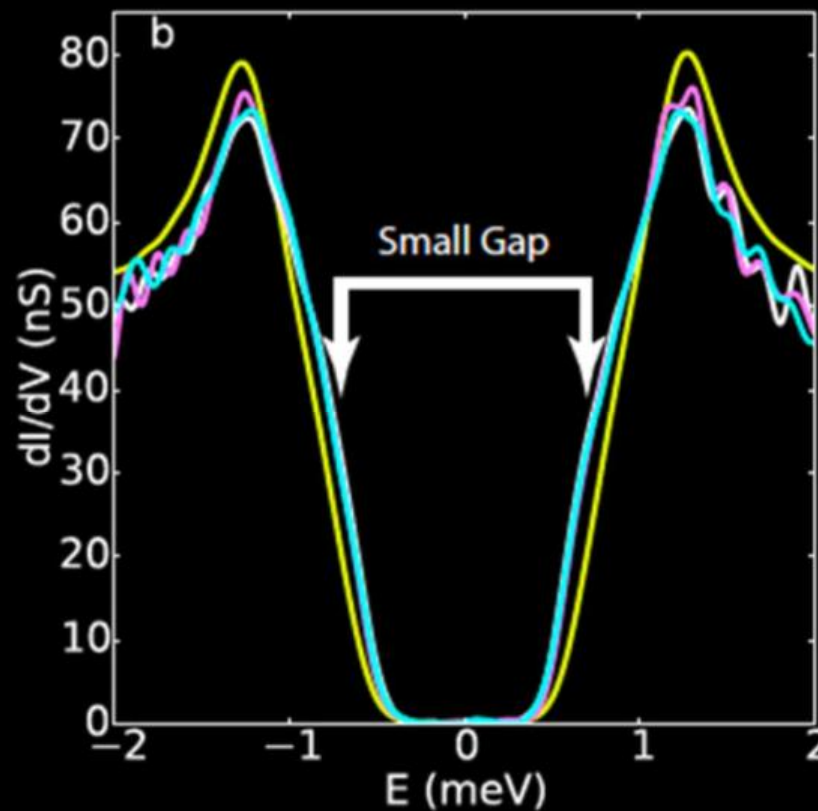
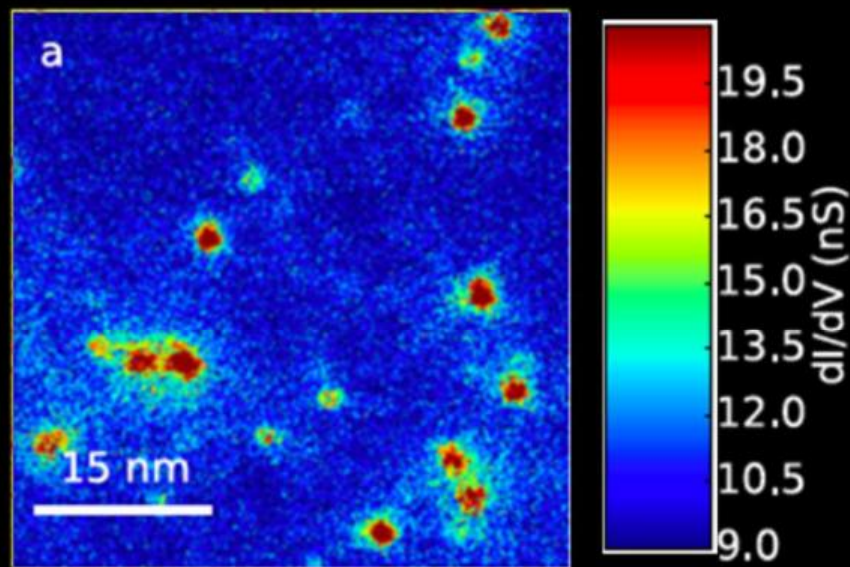
Long-range Shiba bound states – $2H-NbSe_2$



Magnetic impurities:
175 ppm of Fe,
54 ppm of Cr
22 ppm of Mn

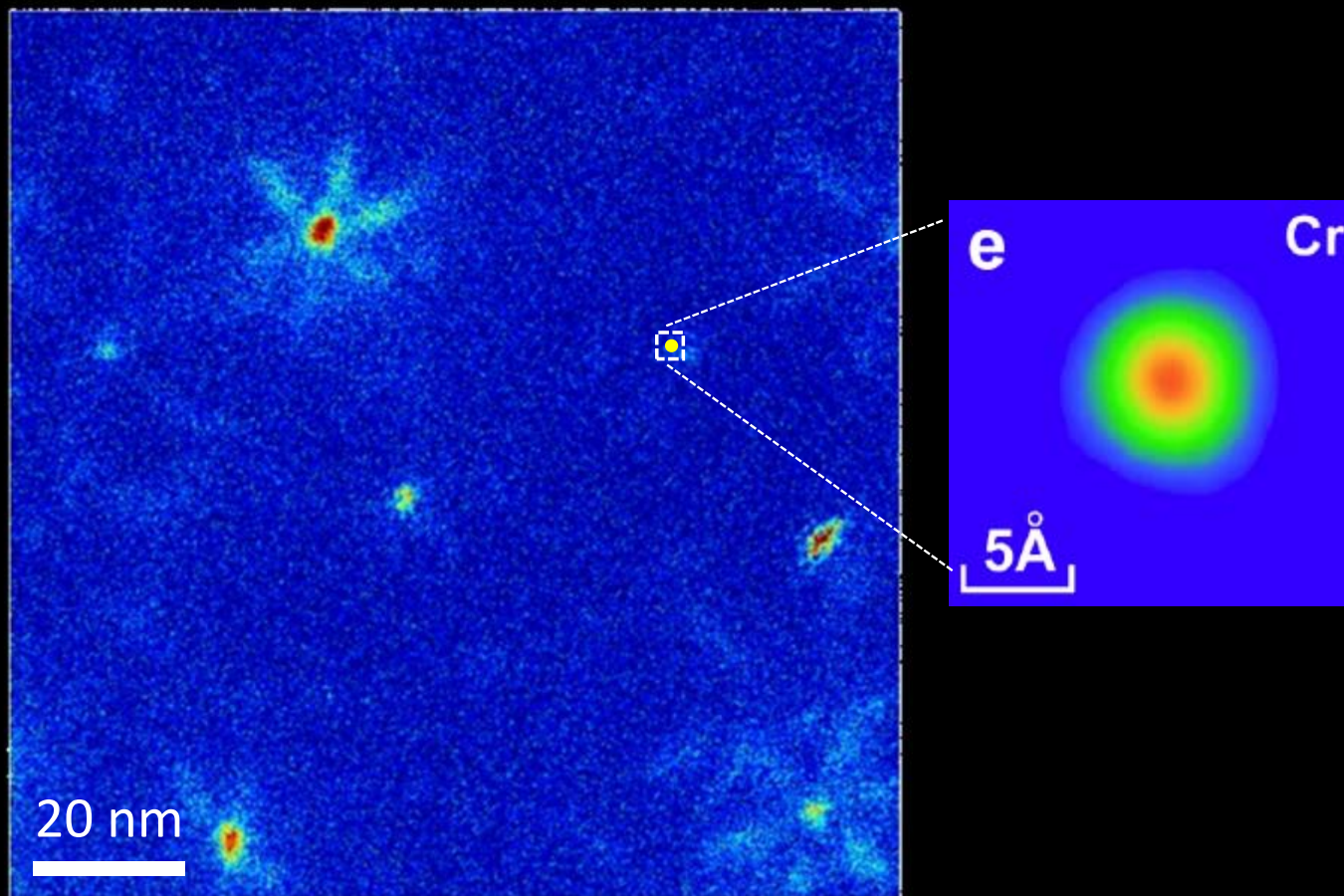
Long-range Shiba bound states – $2H-NbSe_2$

Non-magnetic Ta impurities in $2H-NbSe_2$



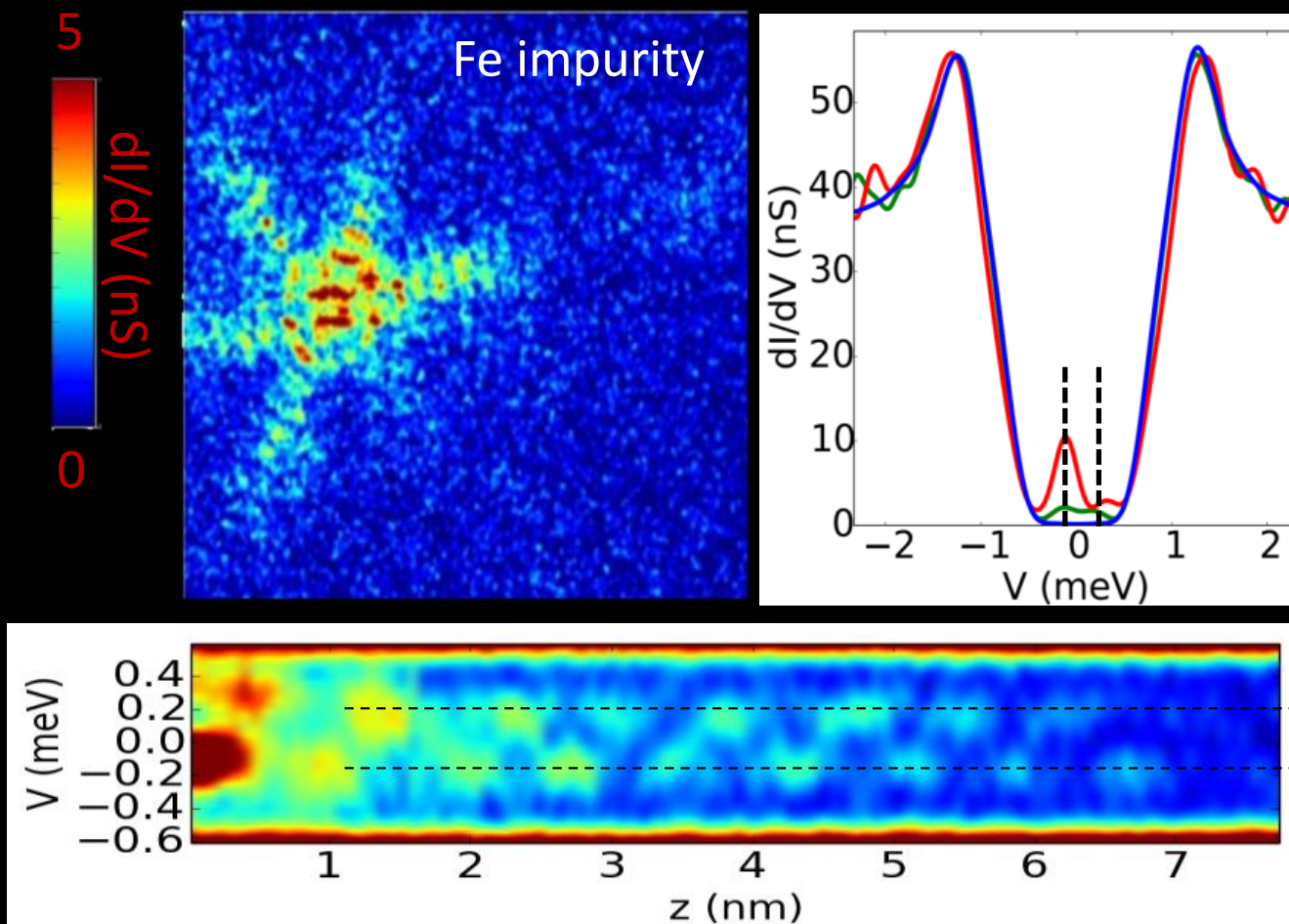
Non-magnetic impurities promote inter-band scattering channel – two band SC

Long-range Shiba bound states – $2H-NbSe_2$



In-gap spectroscopy reveals large scale star shaped features

Long-range Shiba bound states – $2H-NbSe_2$

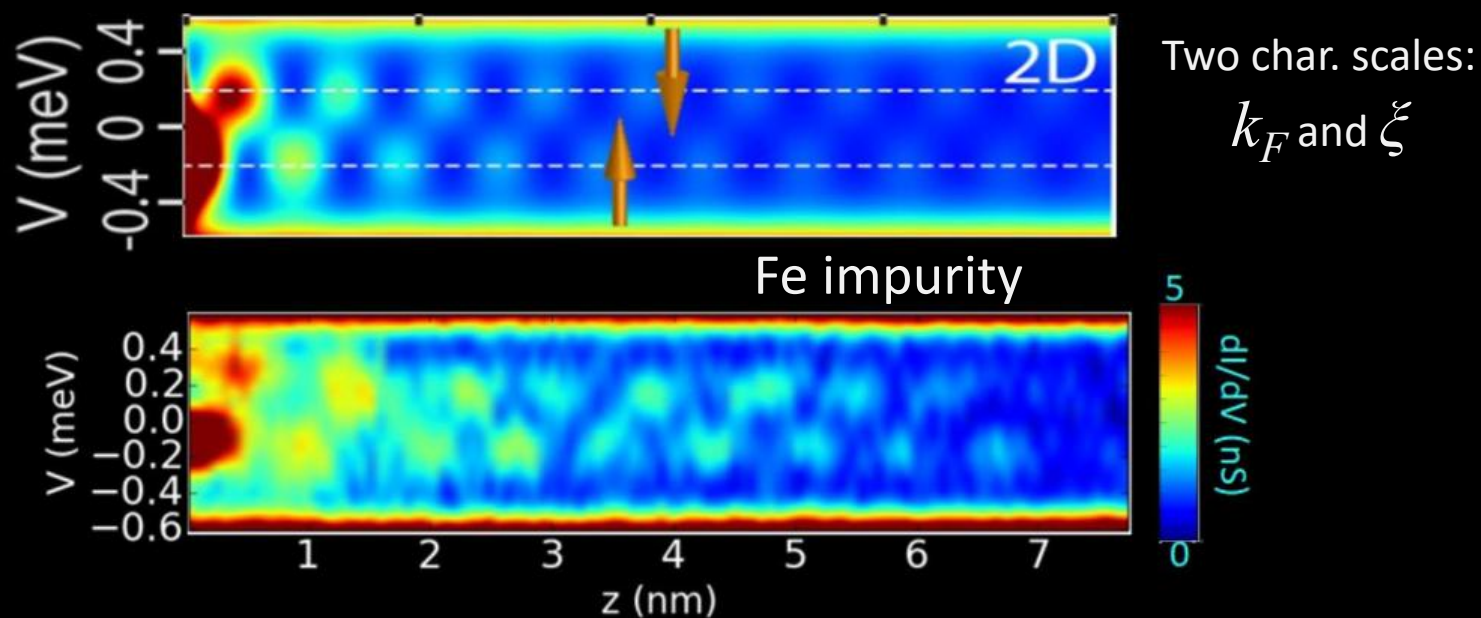


There are 2 Shiba peaks. They oscillate in space with a phase shift.

Long-range Shiba bound states – $2H-NbSe_2$

$$\psi_{\pm} = \frac{1}{\sqrt{N\pi k_F r}} \sin\left(k_F r - \frac{\pi}{4} + \delta^{\pm}\right) e^{-\sin(\delta^+ - \delta^-) r \Delta / \hbar v_F}$$

$$E_S = \Delta \cos(\delta^+ - \delta^-); \quad \tan \delta^{\pm} = K v_0 \pm \frac{JS}{2} v_0$$

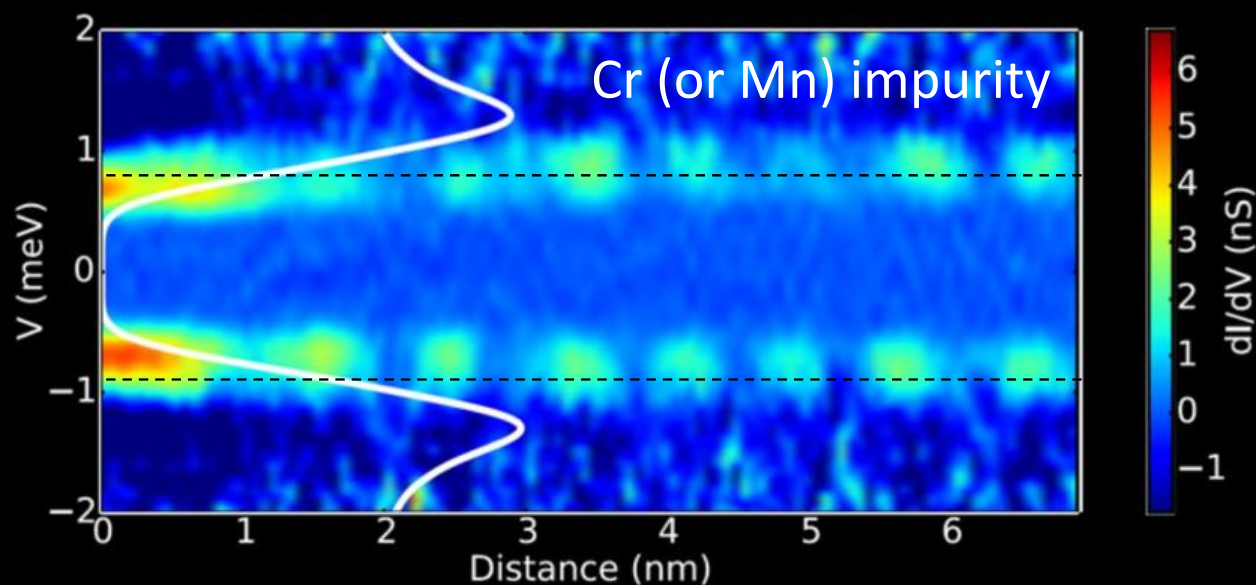


The phase shift is directly related to the position of the Shiba peaks.

Long-range Shiba bound states – $2H-NbSe_2$

$$\psi_{\pm} = \frac{1}{\sqrt{N\pi k_F r}} \sin\left(k_F r - \frac{\pi}{4} + \delta^{\pm}\right) e^{-\sin(\delta^+ - \delta^-) r \Delta / \hbar v_F}$$

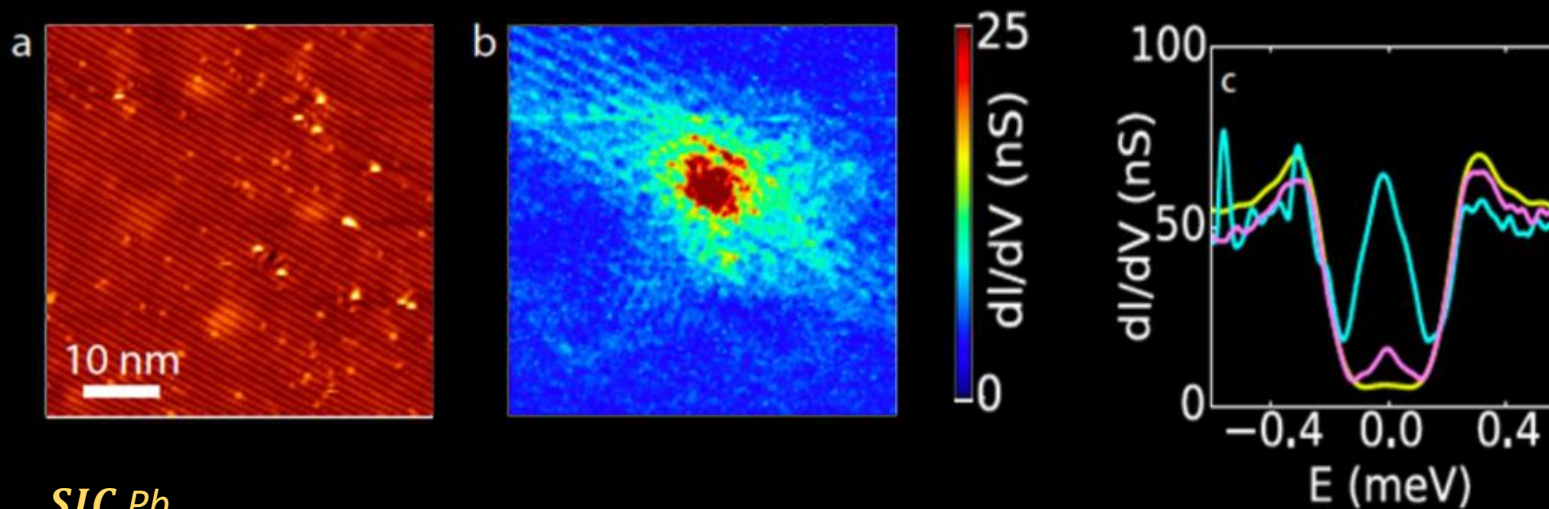
$$E_S = \Delta \cos(\delta^+ - \delta^-); \quad \tan \delta^{\pm} = K v_0 \pm \frac{JS}{2} v_0$$



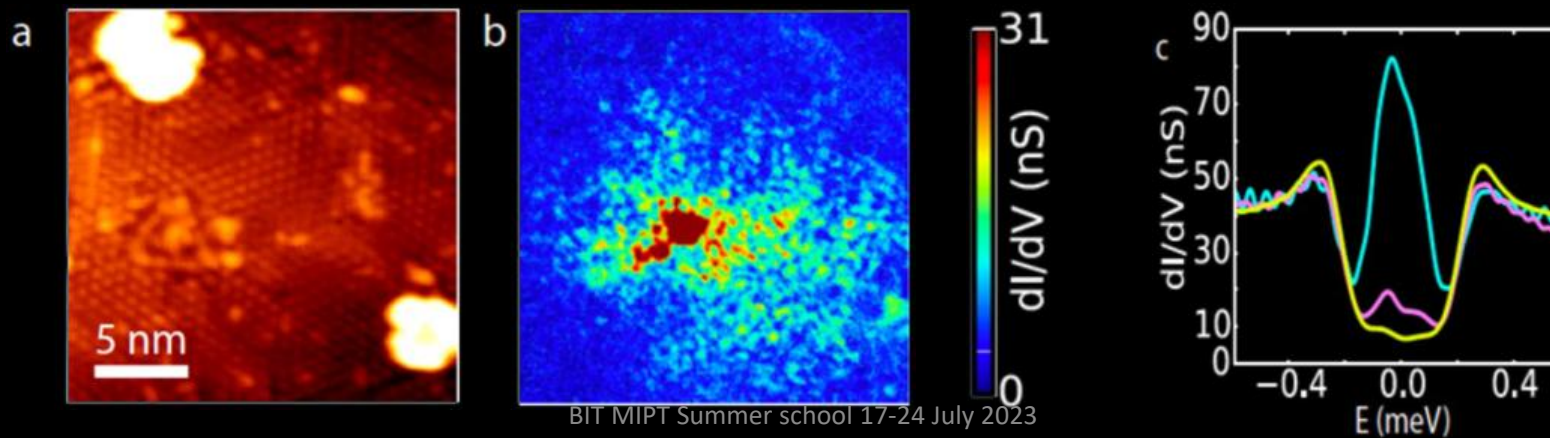
The phase shift is directly related to the position of the Shiba peaks.

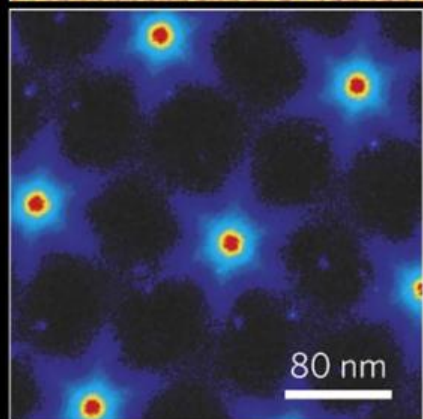
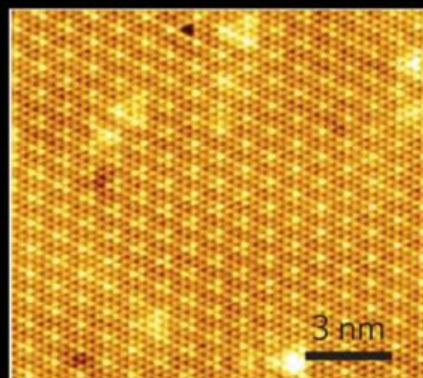
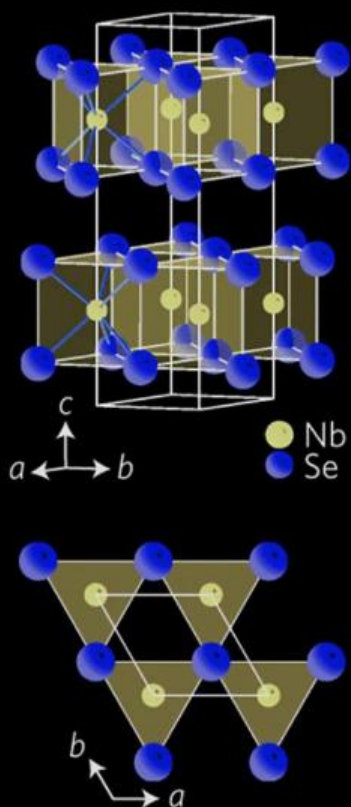
Long-range Shiba bound states – *Pb-ML/Si(111)*

$\sqrt{7} \times \sqrt{3}$ Pb



SIC Pb





nature
physics

LETTERS

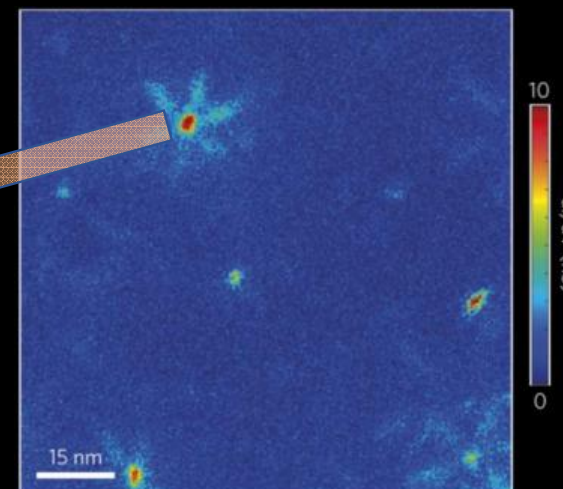
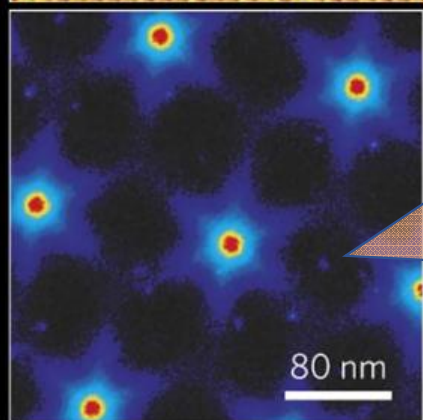
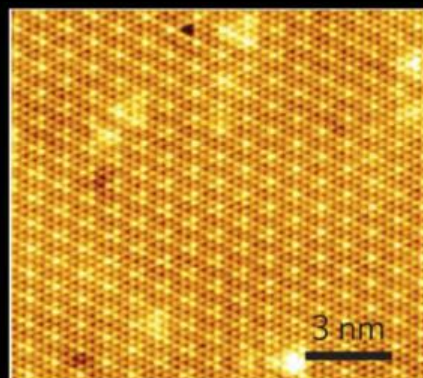
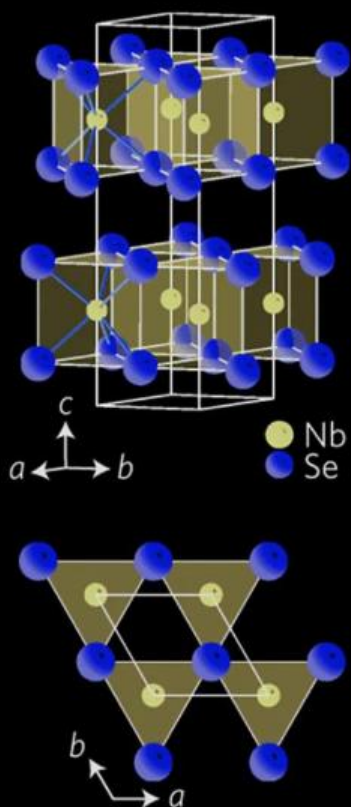
PUBLISHED ONLINE: 12 OCTOBER 2015 | DOI: 10.1038/NPHYS3508

Coherent long-range magnetic bound states in a superconductor

Gerbold C. Ménard¹, Sébastien Guissart², Christophe Brun¹, Stéphane Pons^{1,3}, Vasily S. Stolyarov^{1,4}, François Debontridder¹, Matthieu V. Leclerc¹, Etienne Janod⁵, Laurent Cario⁵, Dimitri Roditchev^{1,3}, Pascal Simon^{2*} and Tristan Cren^{1*}

$$\Delta = 1.1 \text{ mB}$$

$$T = 0.3 \text{ K} < T_C = 7.2 \text{ K}$$



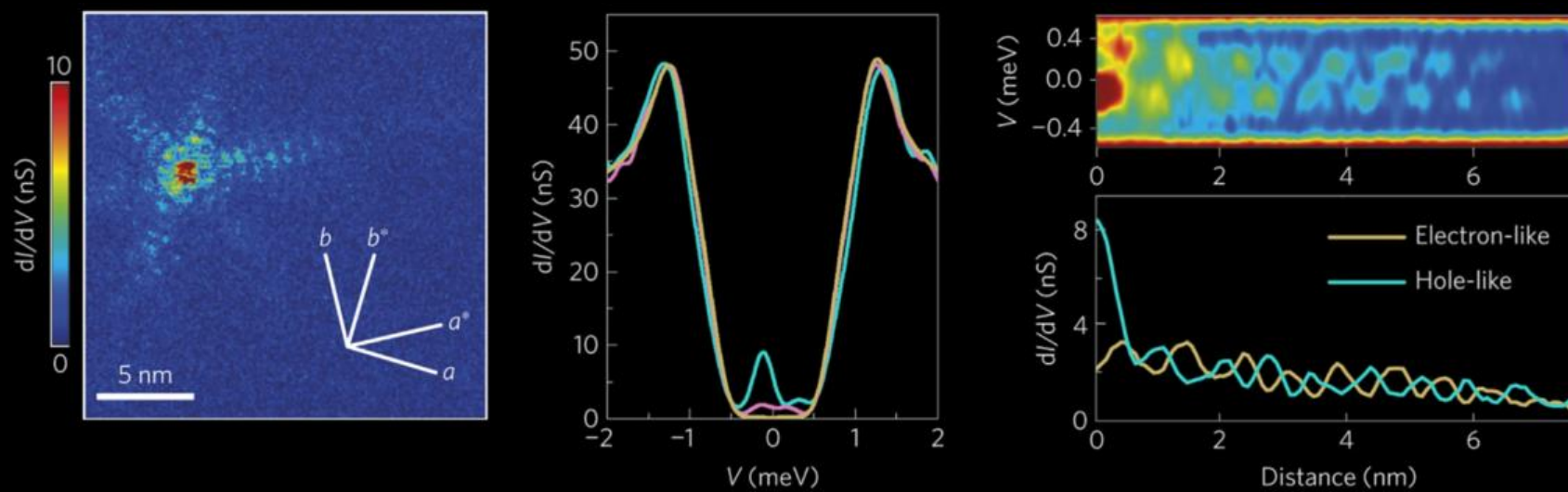
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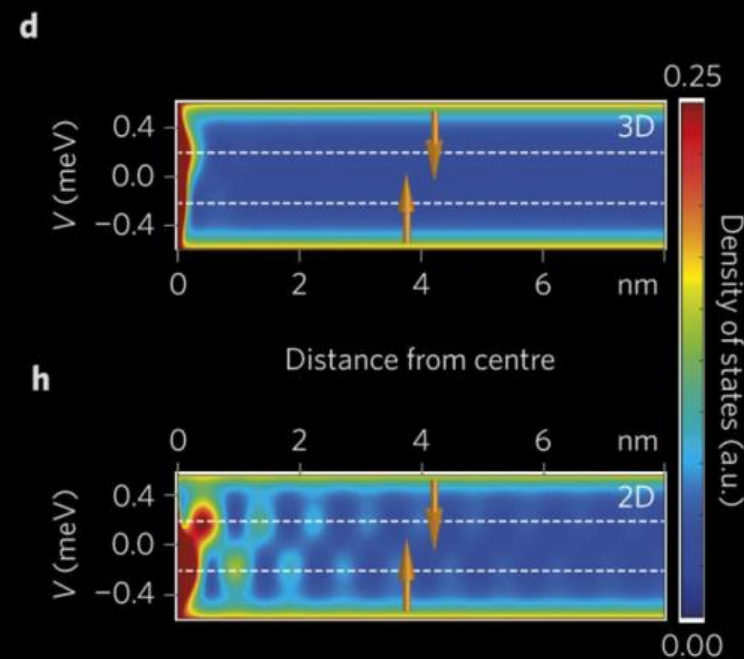
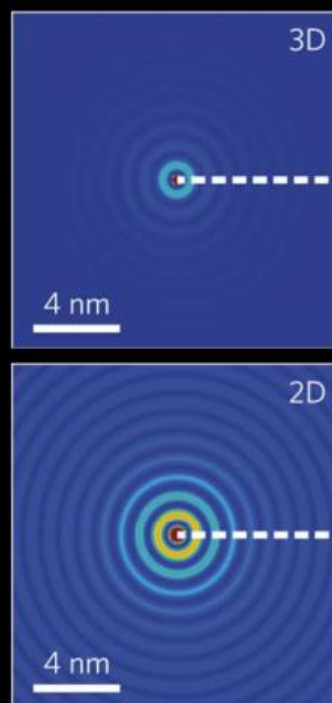
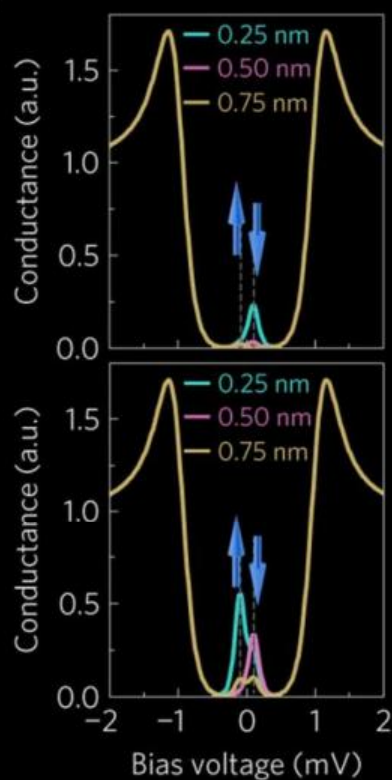
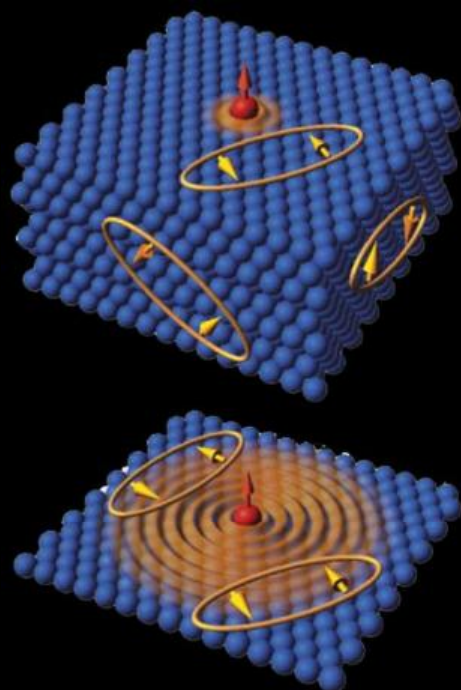
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Coherent long-range magnetic bound states in a superconductor

Gerbold C. Ménard¹, Sébastien Guissart², Christophe Brun¹, Stéphane Pons^{1,3}, Vasily S. Stolyarov^{1,4},
 François Debontridder¹, Matthieu V. Leclerc¹, Etienne Janod⁵, Laurent Cario⁵, Dimitri Roditchev^{1,3},
 Pascal Simon^{2*} and Tristan Cren^{1*}



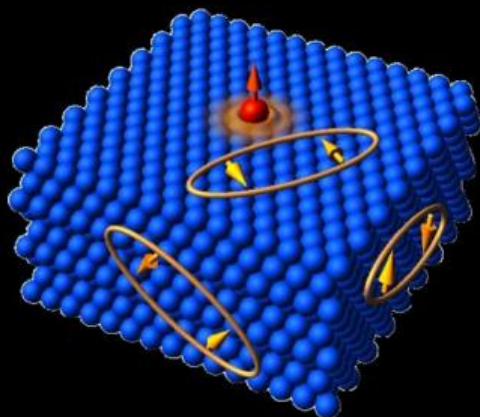
Long-range Shiba bound states – $2H-NbSe_2$



Long-range Shiba bound states – $2H-NbSe_2$

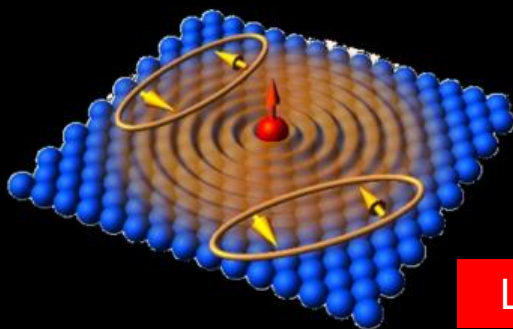
Experimental geometry (coupling, screening):

3D SC, magnetic atoms at the surface



$$\psi_{\pm}^{3D}(r) = \frac{1}{\sqrt{N}} \frac{\sin(k_F r + \delta^{\pm})}{k_F r} e^{-\Delta \sin(\delta^+ - \delta^-) r / \hbar v_F}$$

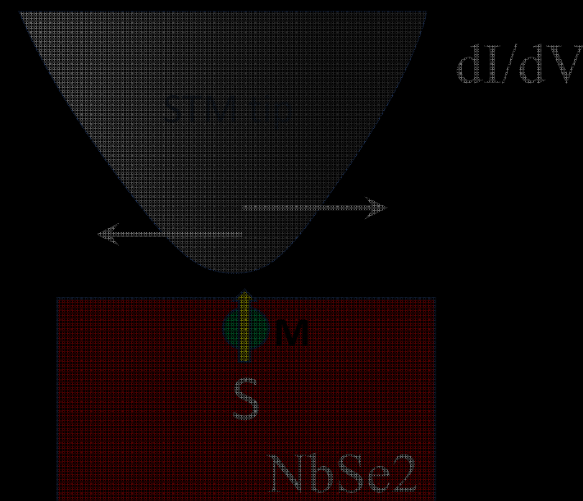
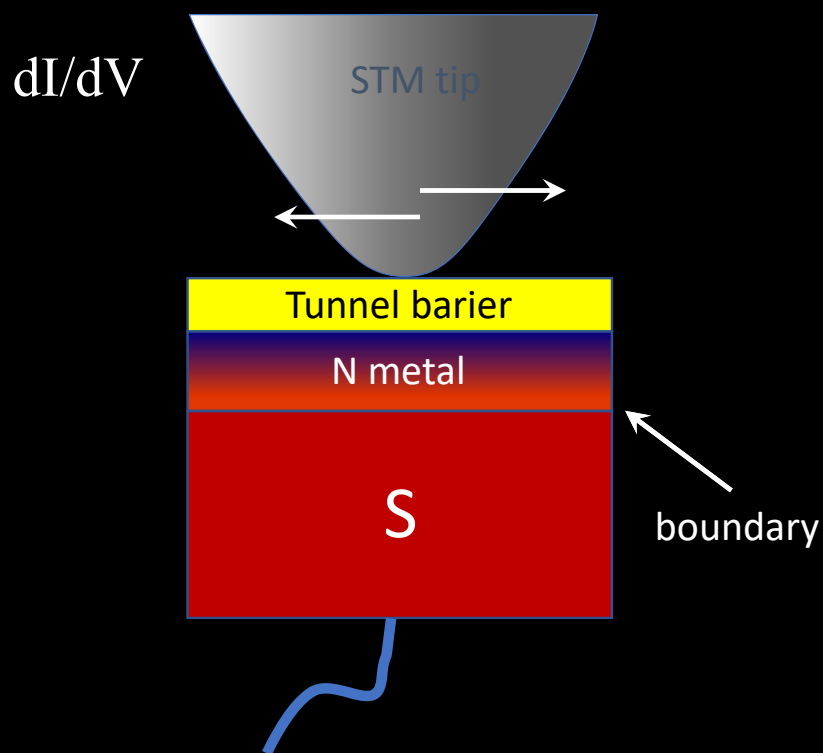
2D SC, magnetic atoms in the matrix



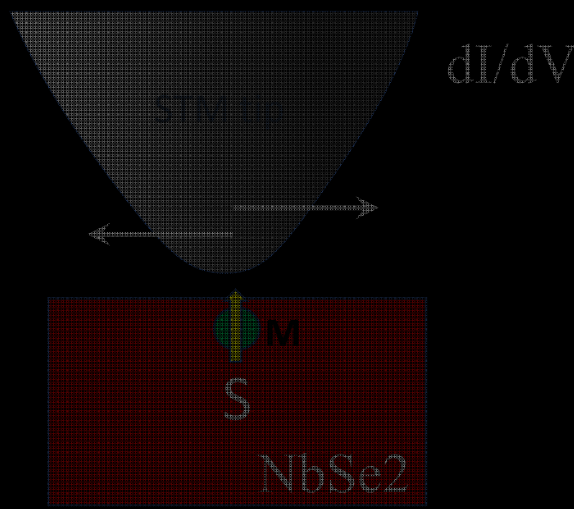
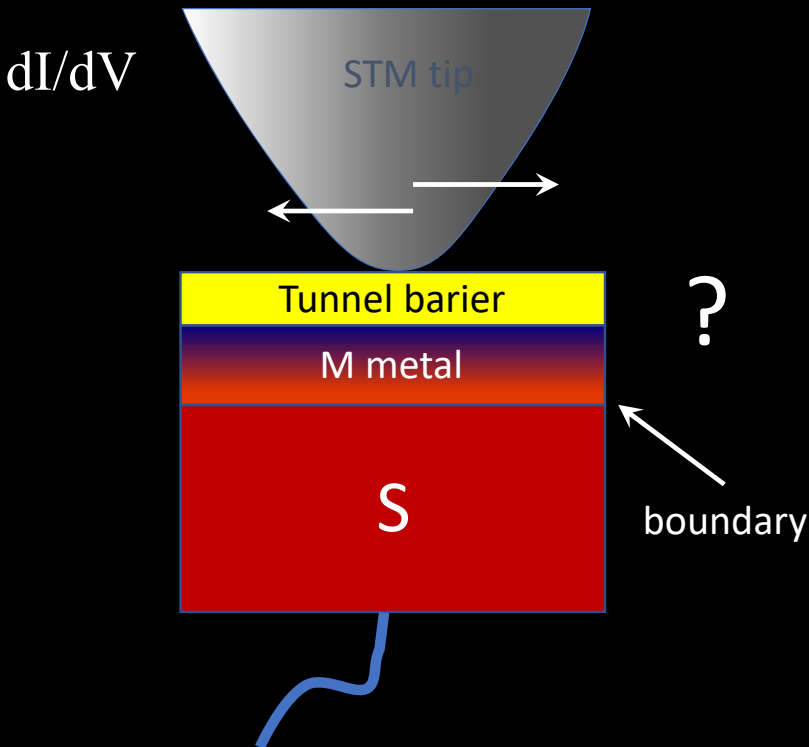
$$\psi_{\pm}^{2D}(r) = \frac{1}{\sqrt{N\pi}} \frac{\sin(k_F r - \frac{\pi}{4} + \delta^{\pm})}{\sqrt{k_F r}} e^{-\Delta \sin(\delta^+ - \delta^-) r / \hbar v_F}$$

Lower dimensionality -> larger extents of YSR bound states

Proximity effect at the superconductor ferromagnet boundary



Proximity effect at the superconductor ferromagnet boundary

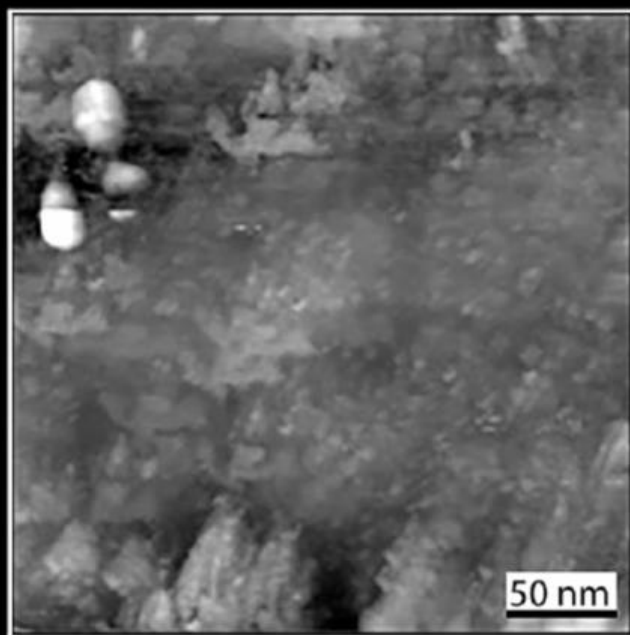




Proximity effect at the superconductor ferromagnet boundary



STM



-3 3
Topography (nm)

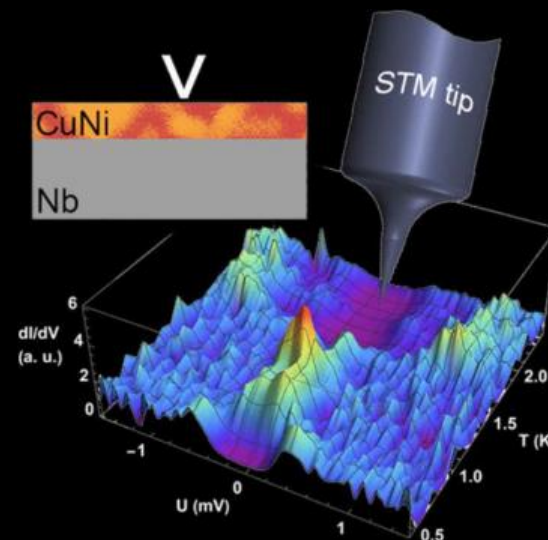
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Letter

Effective Exchange Energy in a Thin, Spatially Inhomogeneous CuNi Layer Proximized by Nb

Vasily Stolyarov,* Vladimir Oboznov, Daniil Kasatonov, Alexey Neilo, Sergey Bakurskiy, Nikolay Klenov, Igor Soloviev, Mikhail Kupriyanov, Alexander Golubov, Tristan Cren, and Dimitri Roditchev

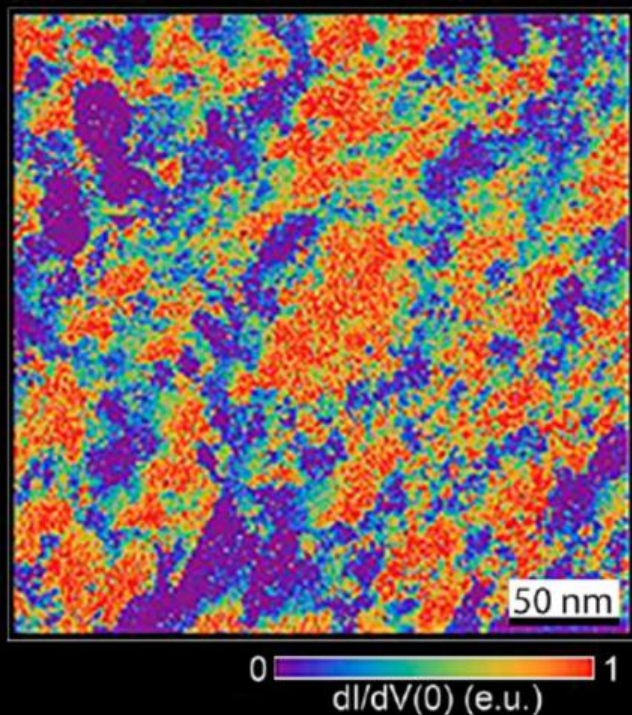




Proximity effect at the superconductor ferromagnet boundary



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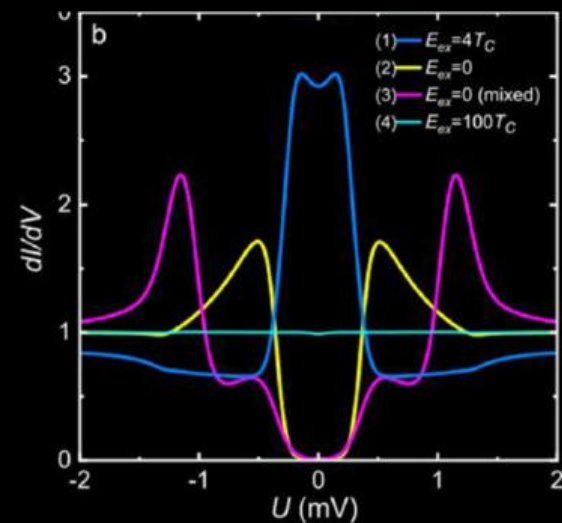
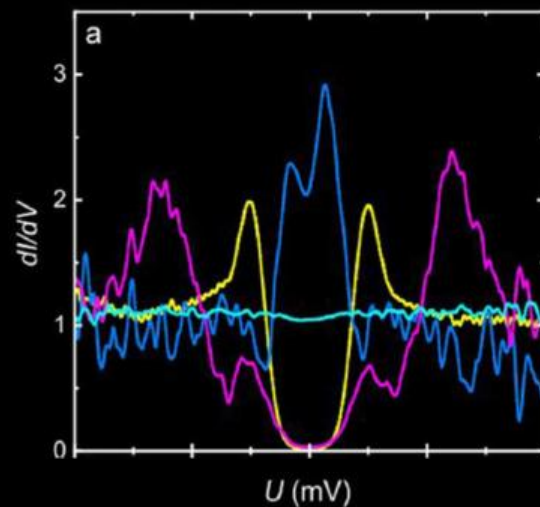
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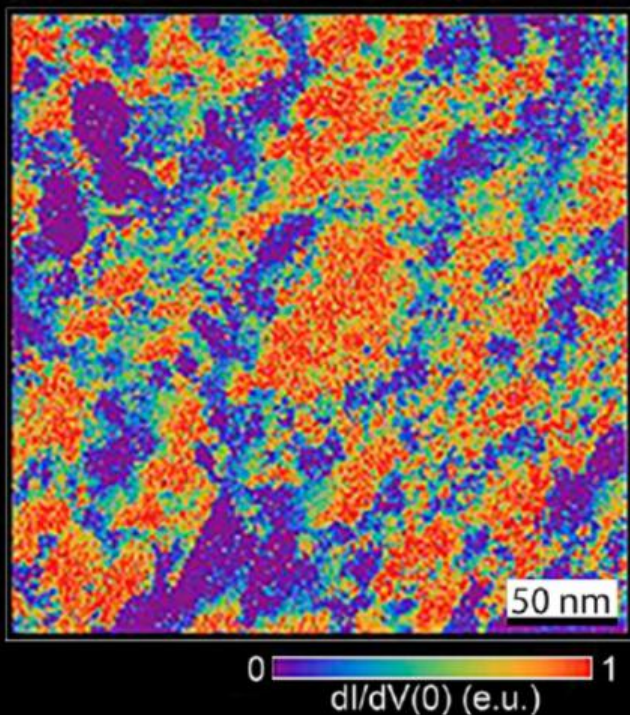
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curve number	d_{F_1} nm	E_{ex}	ξ_{F_1} nm	ρ_{F_1} $\mu\Omega$ cm	γ_B
1	7	$4T_c$	35	12.9	3
2	11	0	20	3.8	0.1
3(0.6)	11	0	20	3.8	0.1
3(0.4)	7	0	20	9.1	0.1
4	7	$100T_c$	35	12.9	3

